

WIMP Dark Matter

&

Halo-Independent Analysis of Direct Detection Data

Paolo Gondolo

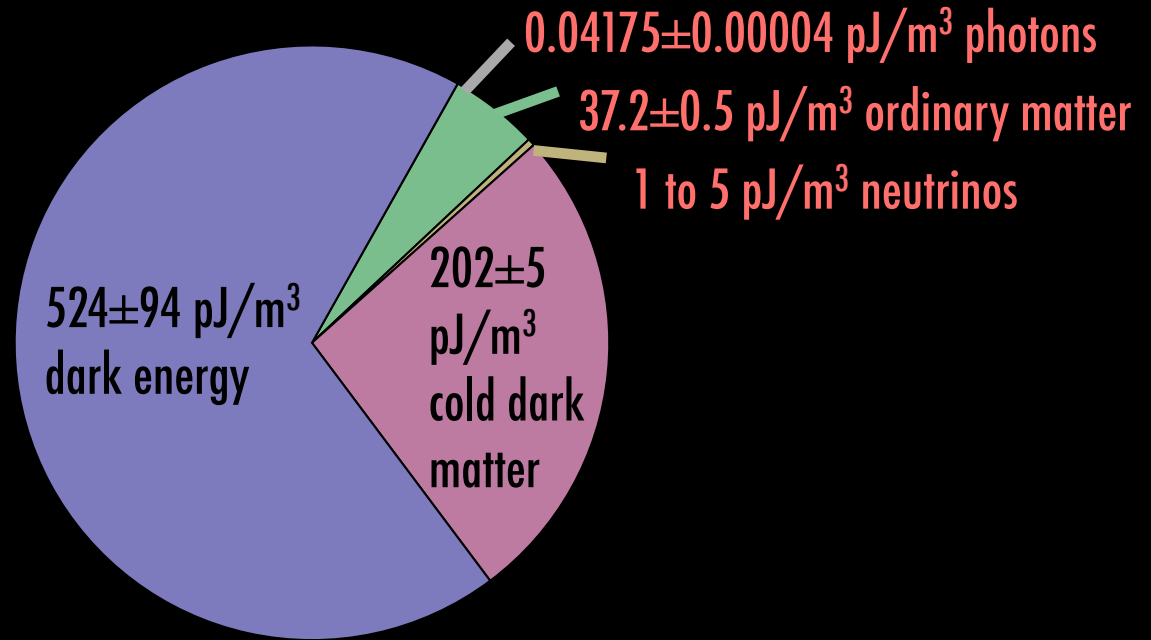
University of Utah

The Magnificent WIMP

(Weakly Interacting Massive Particle)

- One naturally obtains the right cosmic density of WIMPs

Thermal production in hot primordial plasma.



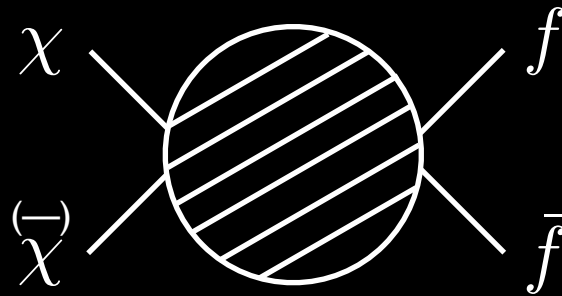
- One can experimentally test the WIMP hypothesis

The same physical processes that produce the right density of WIMPs make their detection possible

Cosmic density of thermal WIMPs

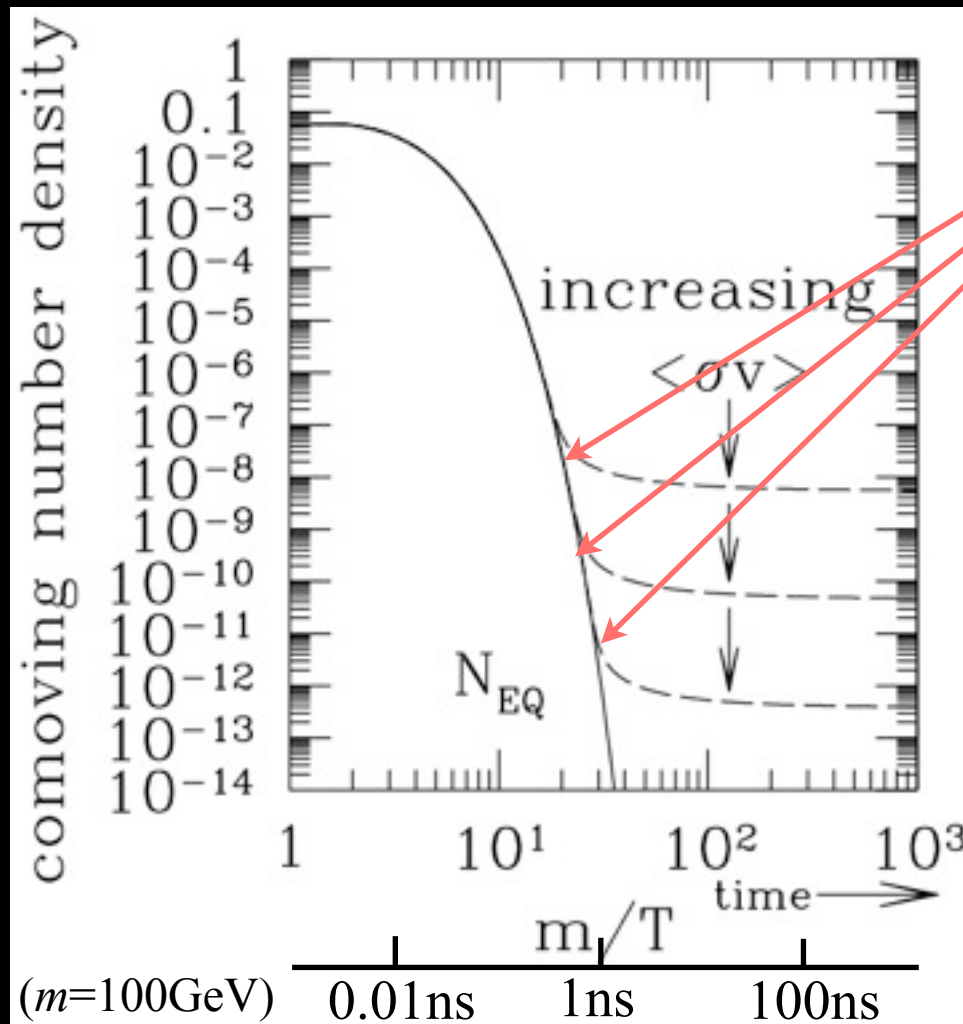
- At early times, WIMPs are produced in e^+e^- , $\mu^+\mu^-$, etc collisions in the hot primordial soup [*thermal production*].

$$e^+ + e^-, \mu^+ + \mu^-, \text{etc.} \leftrightarrow \chi + \bar{\chi}$$



- WIMP production ceases when the production rate becomes smaller than the Hubble expansion rate [*freeze-out*].
- After freeze-out, there is a constant number of WIMPs in a volume expanding with the universe.

Cosmic density of thermal WIMPs



freeze-out

$$\Gamma_{\text{ann}} \equiv n \langle \sigma v \rangle \sim H$$

annihilation rate expansion rate

$$\Omega_{\chi} h^2 \simeq \frac{3 \times 10^{-27} \text{cm}^3/\text{s}}{\langle \sigma v \rangle_{\text{ann}}}$$

$$\Omega_{\chi} h^2 = \Omega_{\text{cdm}} h^2 \simeq 0.1143$$

for $\langle \sigma v \rangle_{\text{ann}} \simeq 3 \times 10^{-26} \text{cm}^3/\text{s}$

*This is why they are called Weakly Interacting Massive Particles
(WIMPless candidates are WIMPs!)*

Cosmic density of thermal WIMPs

- In general, $\langle\sigma v\rangle$ is a complicated function of the WIMP mass m and the WIMP velocity v , including resonances, thresholds, and coannihilations.
- At small v , $\langle\sigma v\rangle$ can be expanded as

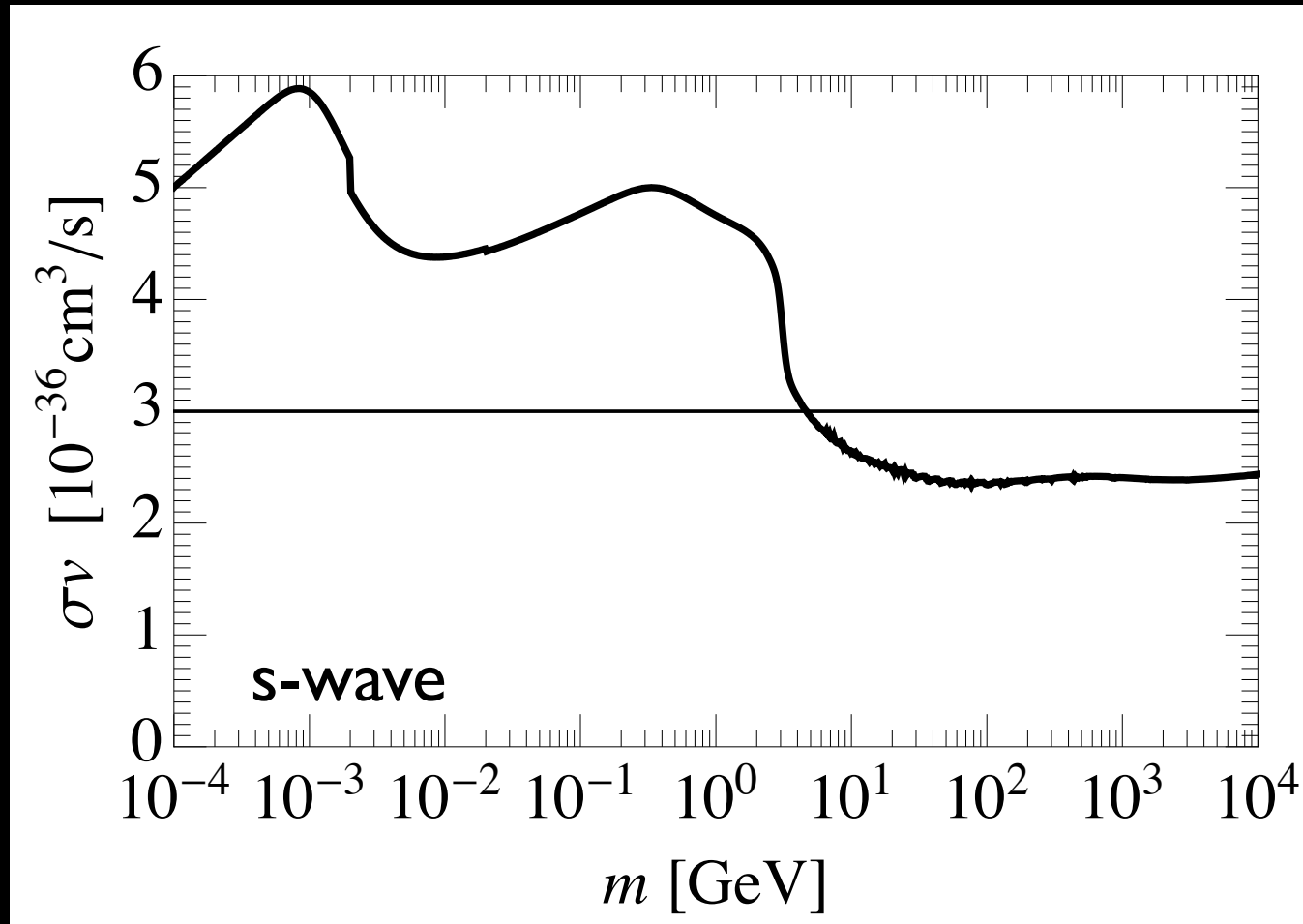
$$\langle\sigma v\rangle = a + bv^2 + \dots \quad \text{s-wave}$$

$$\langle\sigma v\rangle = bv^2 + cv^4 + \dots \quad \text{p-wave}$$

(These expansions are not good near a resonance or threshold.)

Cosmic density of thermal WIMPs

$\langle\sigma v\rangle=\text{const}$ required for right cosmic density

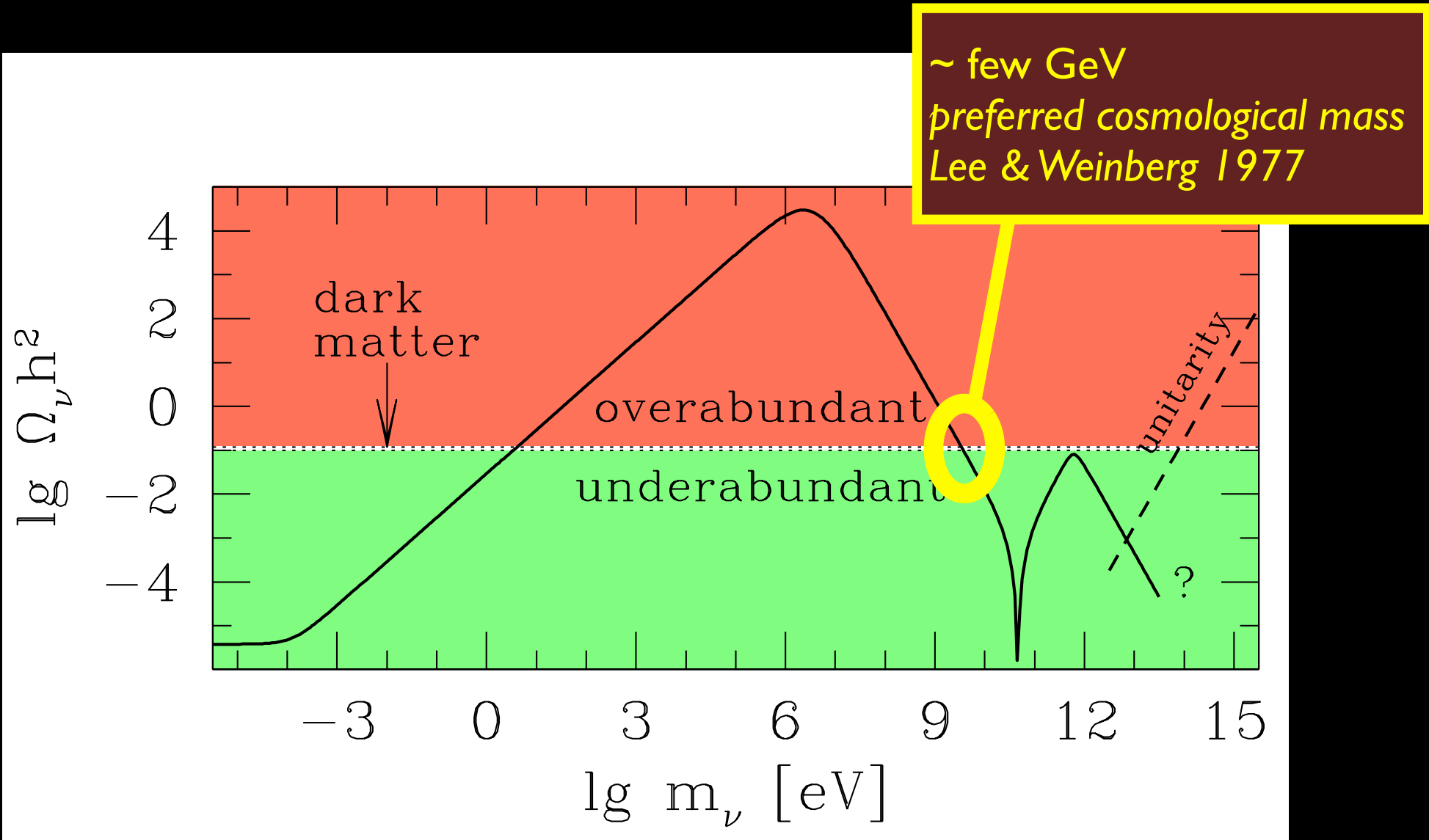


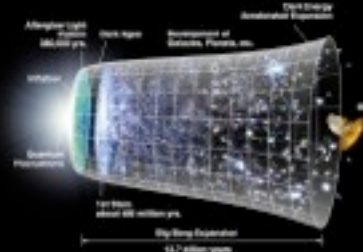
Steigman, Dasgupta, Beacom 2012

Gondolo, Steigman (in prep.)

Cosmic density of thermal WIMPs

Fourth-generation Standard Model neutrino

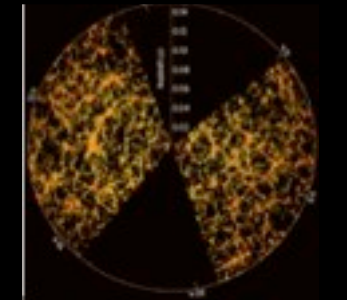
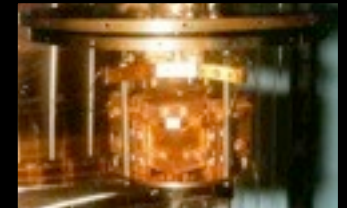




Cosmic density

A Feynman diagram representing a box process. It features a central circle filled with diagonal hatching. Four external lines are connected to the circle: a top-left line labeled χ , a top-right line labeled f , a bottom-left line labeled $\chi^{(-)}$, and a bottom-right line labeled $f^{(-)}$. Above the circle, a horizontal arrow points from left to right.

Direct detection

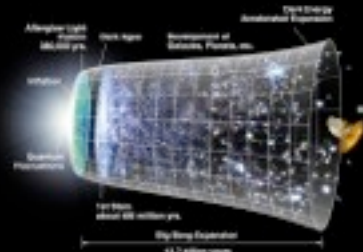
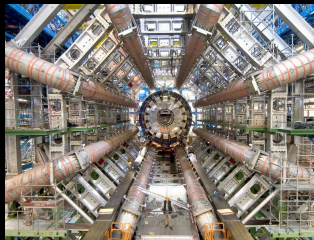


Large scale structure

Scattering

Production

Colliders

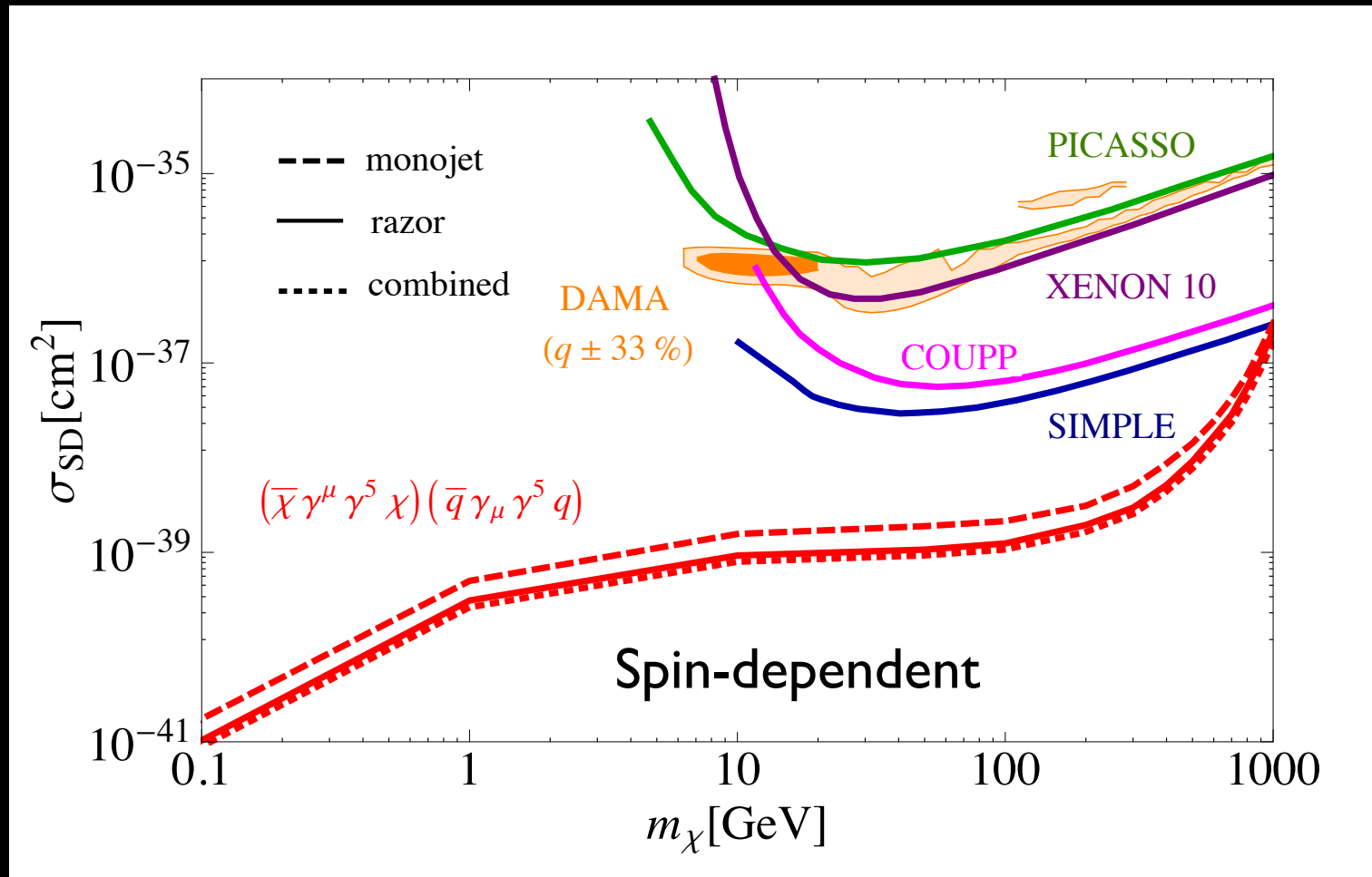


Cosmic density

The power of the WIMP hypothesis

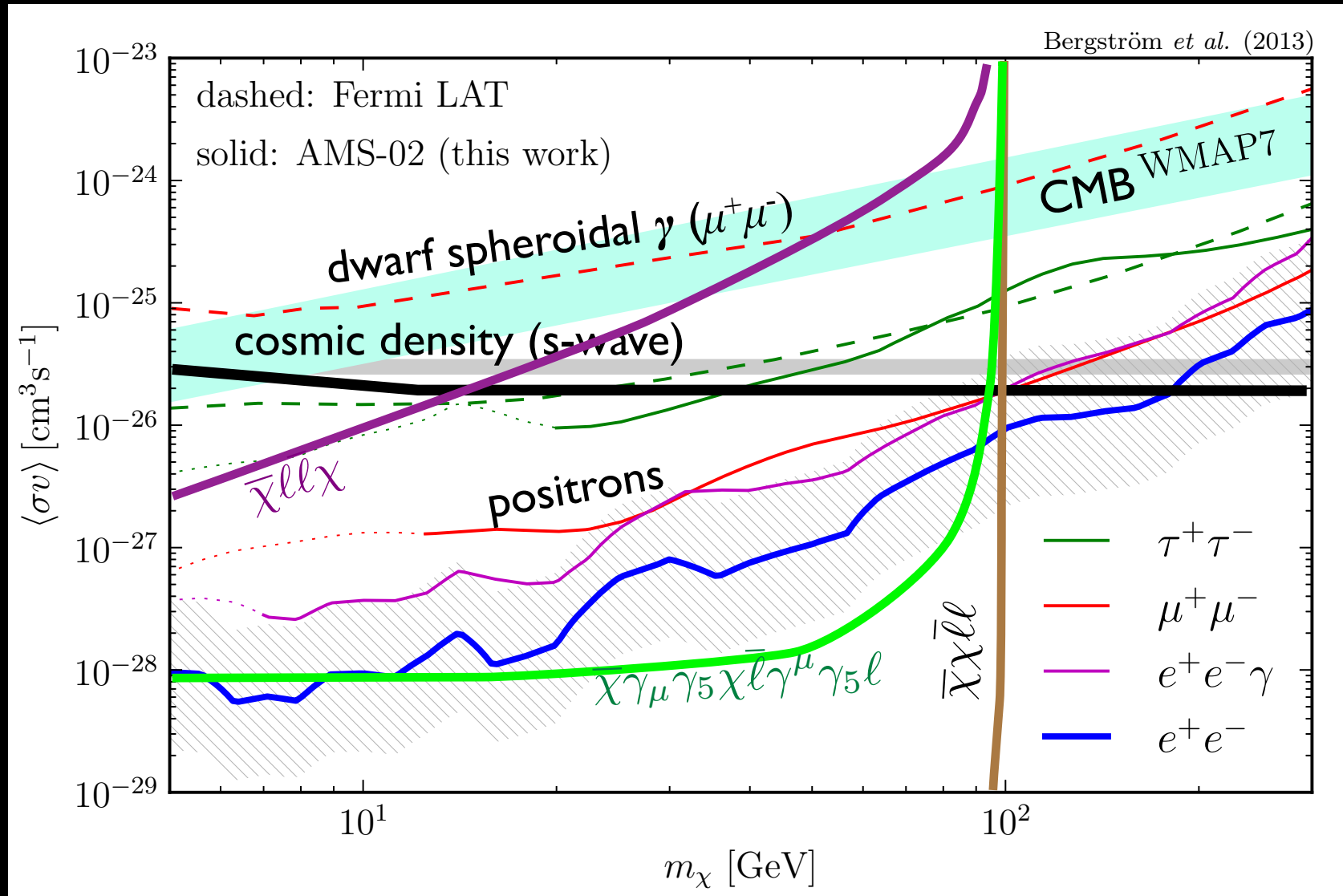
Constraints on scattering cross section

Direct detection and LHC



Fox et al 2012

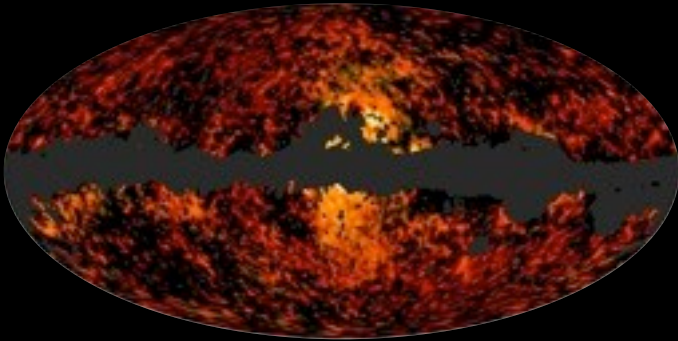
γ -rays, cosmological ionization, positrons, and LHC



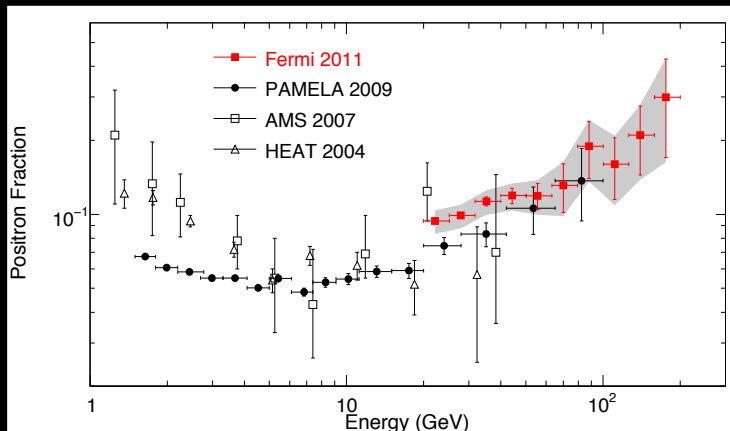
Kopp, Fox, Harnik, Tait 2011 & Bergstrom et al 2013

Evidence for WIMP dark matter?

WMAP/Planck haze



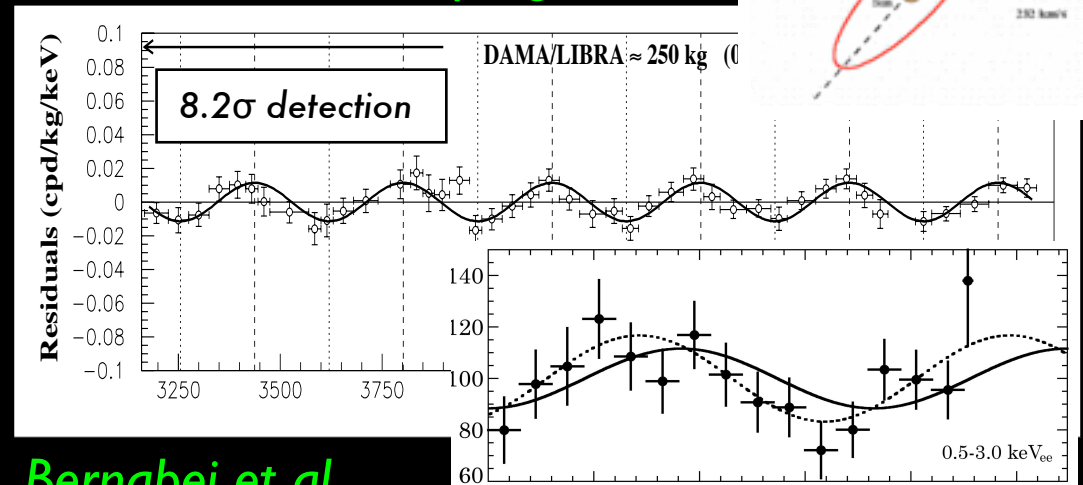
Positron excess



Adriani et al 2009; Ackerman et al 2011; Aguilar et al 2013

Annual modulation

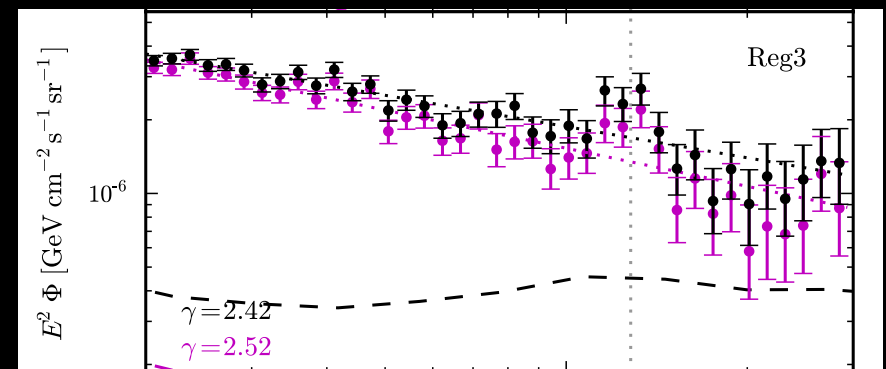
Drukier, Freese, Spergel 1986



Bernabei et al 1997-2012

Aalseth et al 2011

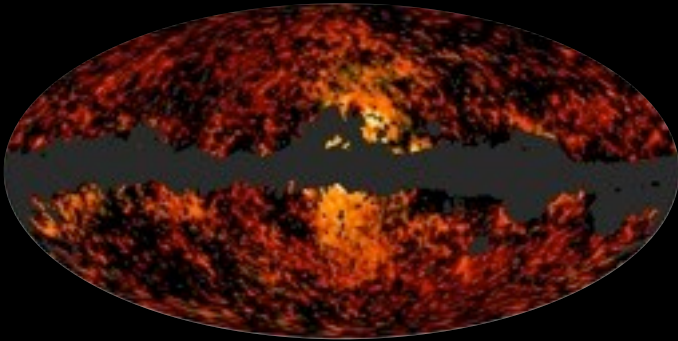
130 GeV γ -ray line



Weniger 2012

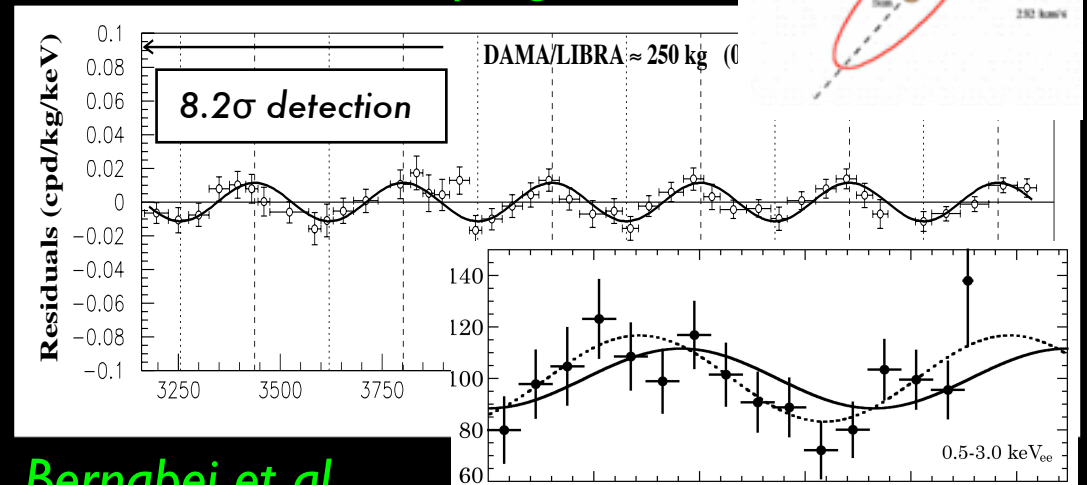
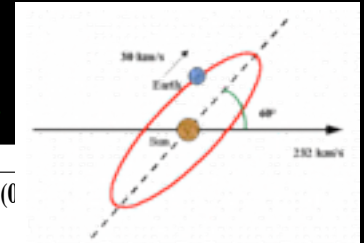
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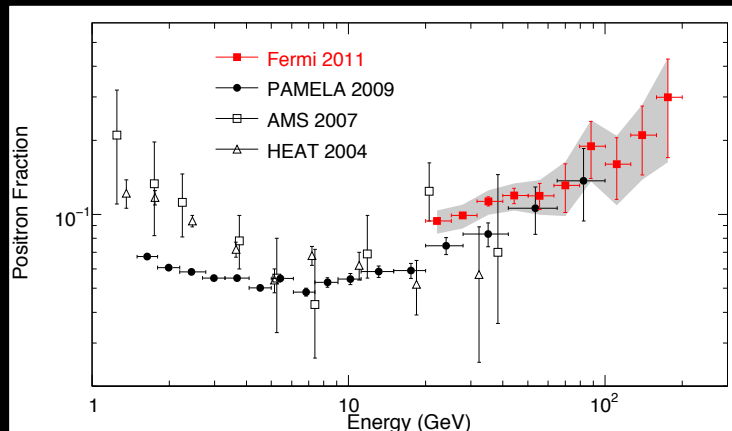
Drukier, Freese, Spergel 1986



*Bernabei et al
1997-2012*

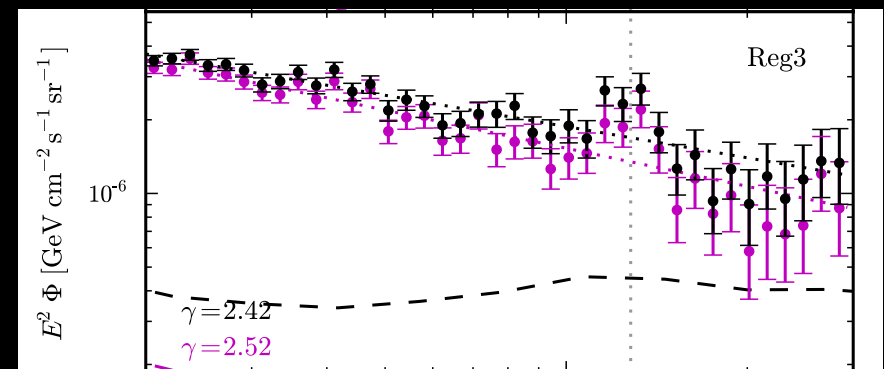
Aalseth et al 2011

Positron excess



Adriani et al 2009; Ackerman et al 2011; Aguilar et al 2013

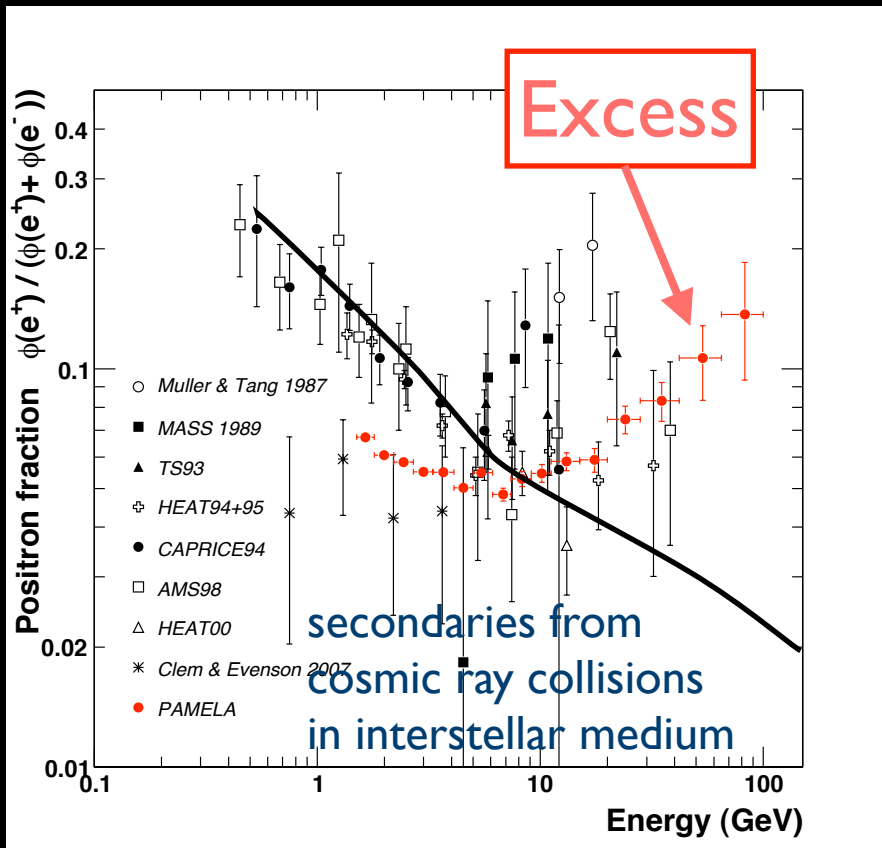
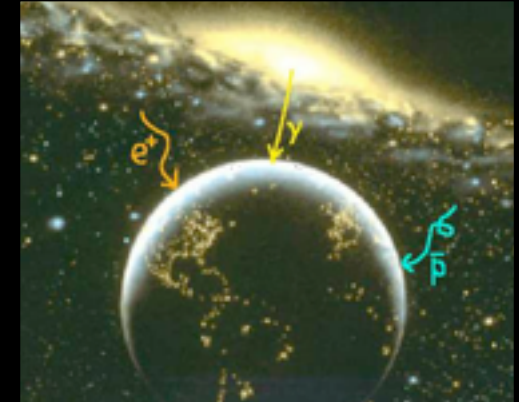
130 GeV γ -ray line



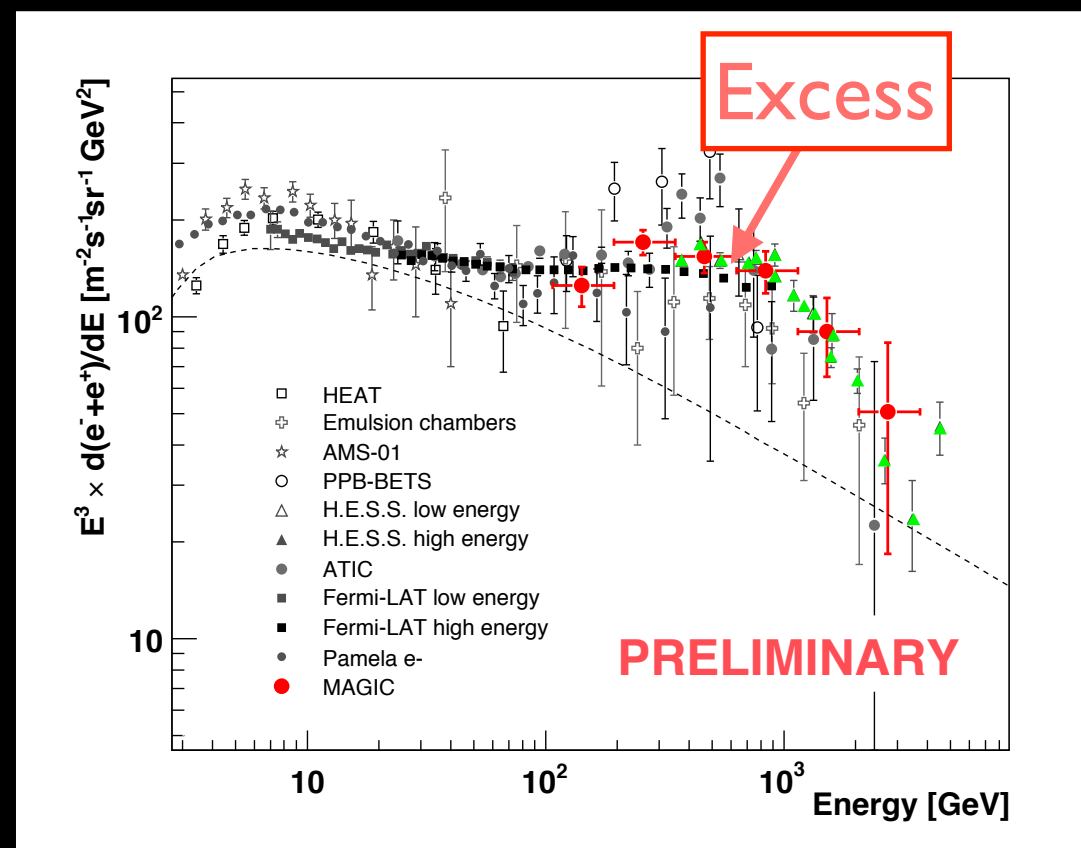
Weniger 2012

Excess in cosmic ray positrons

High energy cosmic ray positrons are more than expected



Adriani et al. [PAMELA], arXiv: 0810.4995



Borla Tridon et al [MAGIC], arXiv: 1110.4008

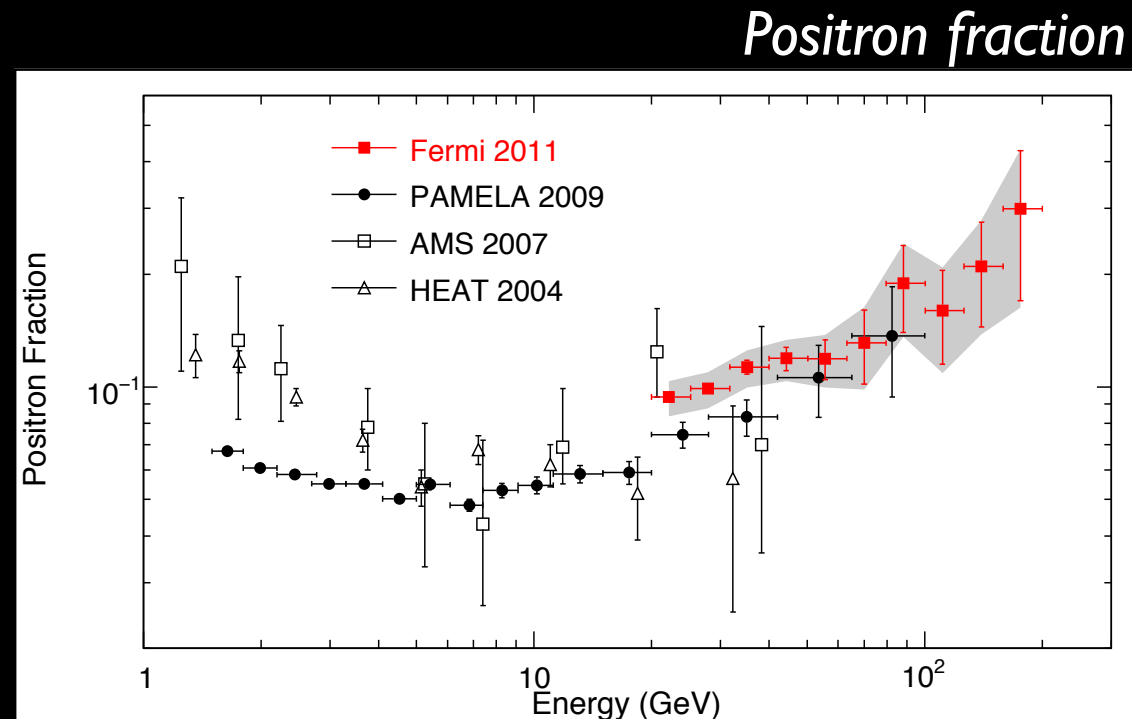
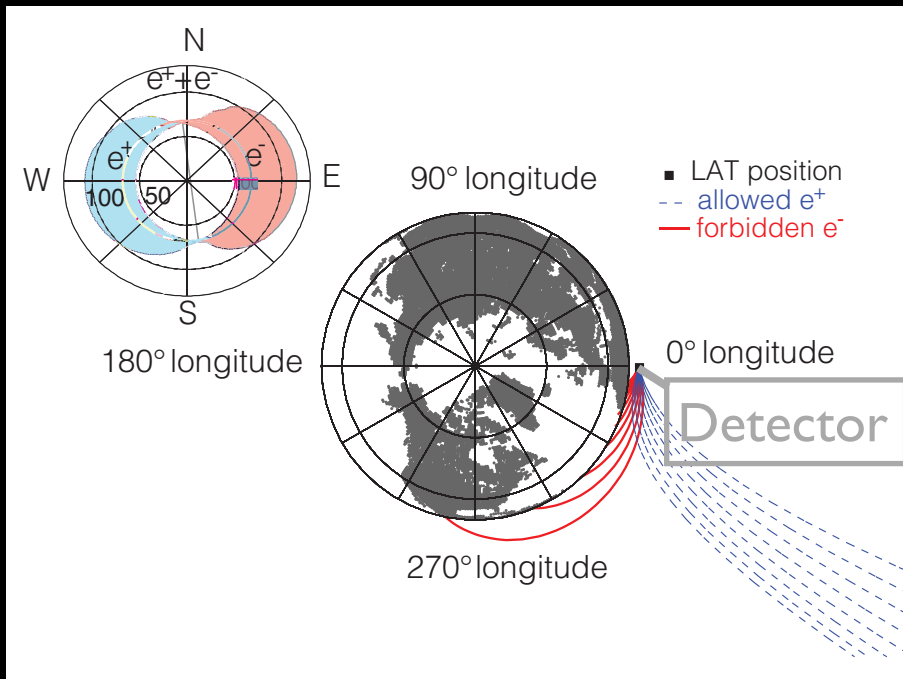
Cosmic ray positrons

Fermi-LAT confirms and extends the positron excess

Ackermann et al, 1109.0521

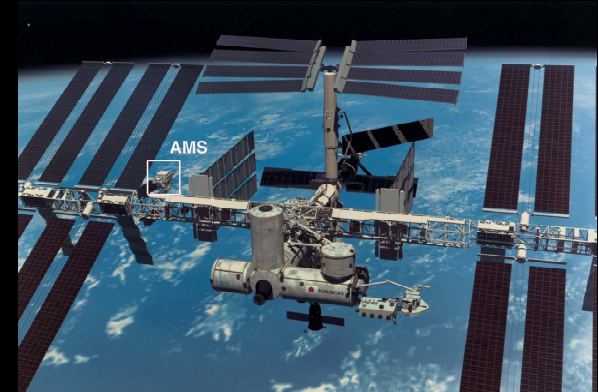
Use the biggest magnet on Earth: the geomagnetic field!

Daniel, Stephens 1965; Müller, Tang 1987

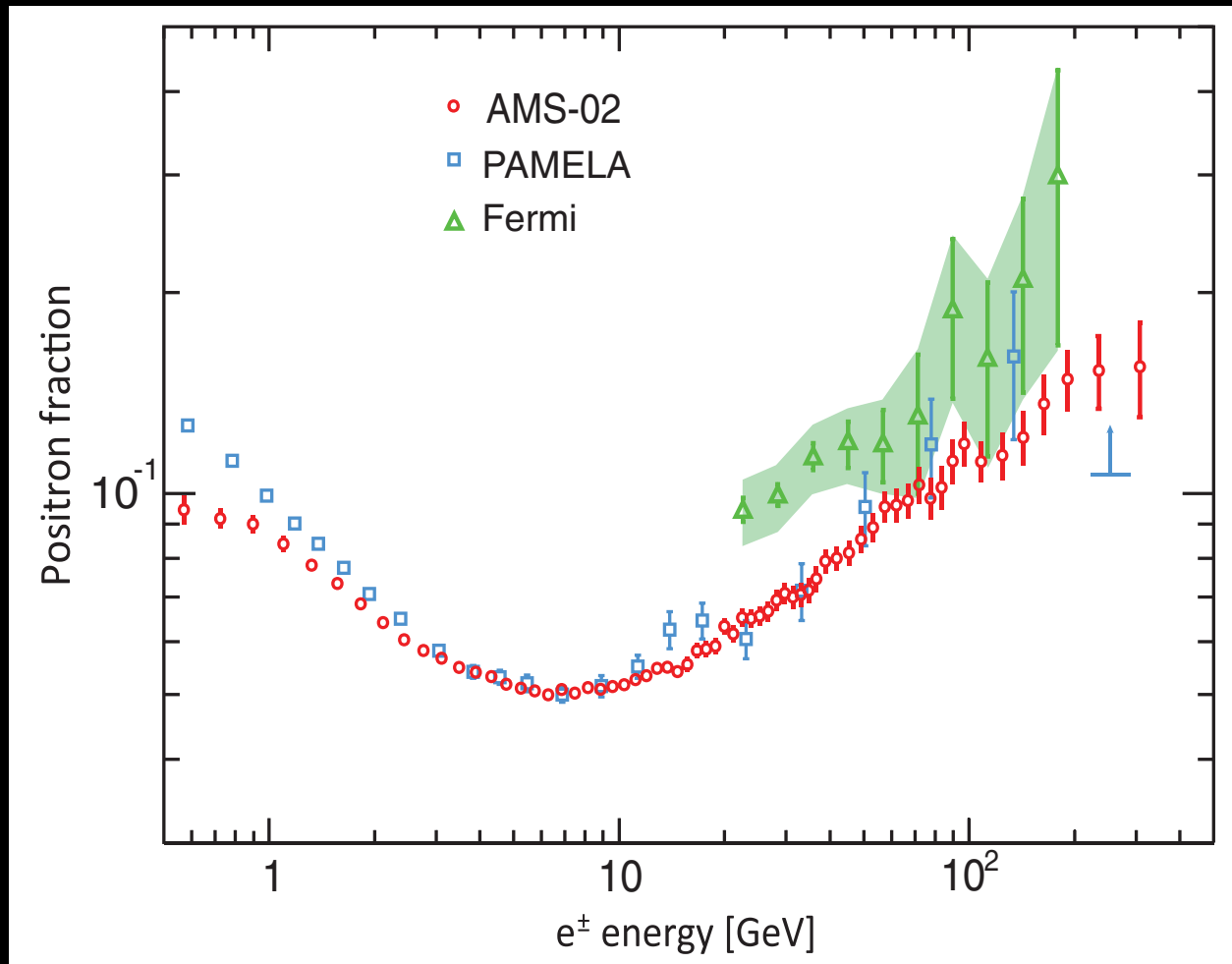


Excess in cosmic ray positrons

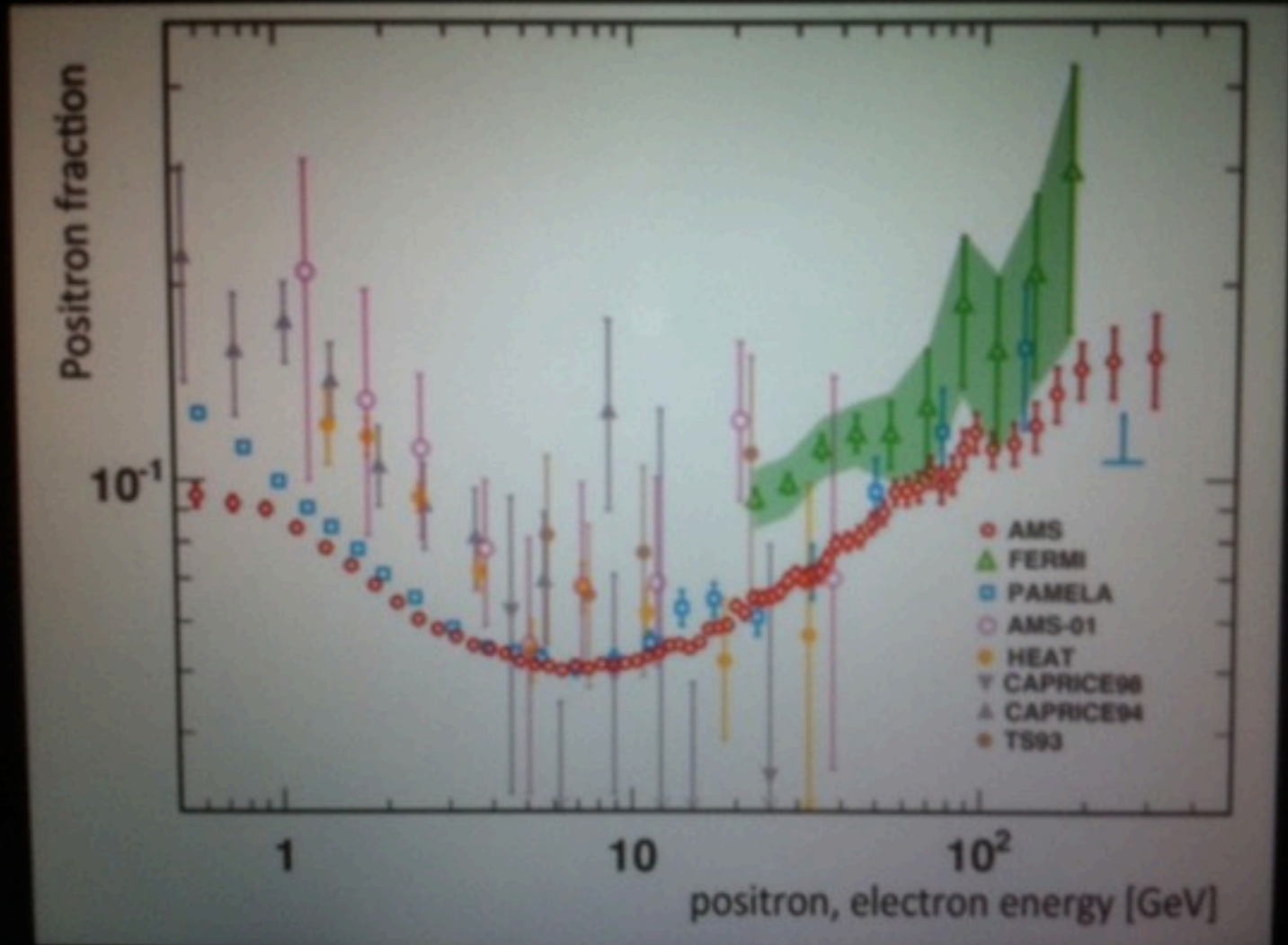
AMS-02 provides data with exquisite precision



Aguilar et al (AMS-02) 2013



Excess in cosmic ray positrons



Ting 2013

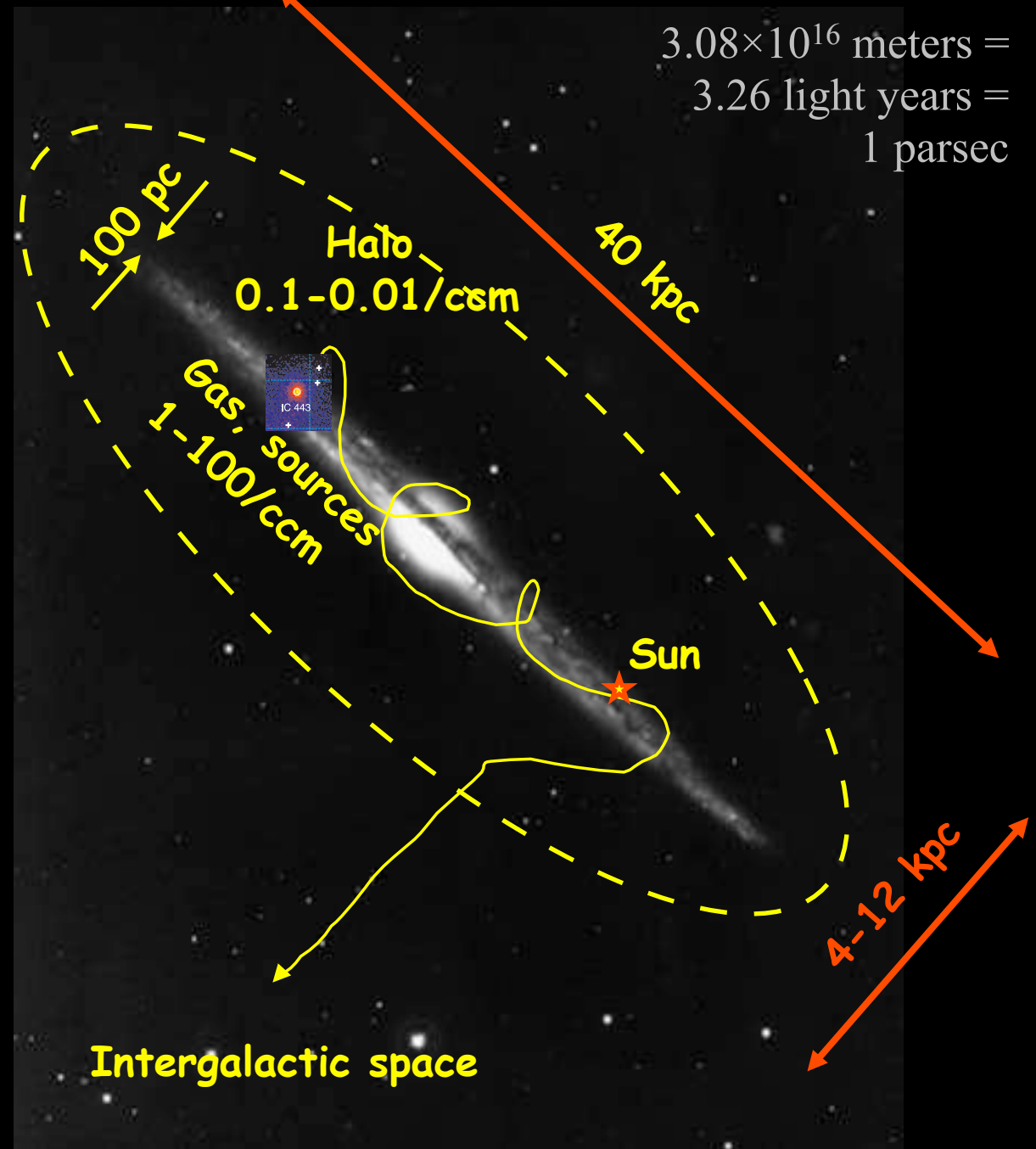
Excess in cosmic ray positrons

Galactic cosmic rays

- Primary cosmic rays (p, ^4He , C, N, O, ..., Fe, ^{64}Ni) are produced in supernova remnants.

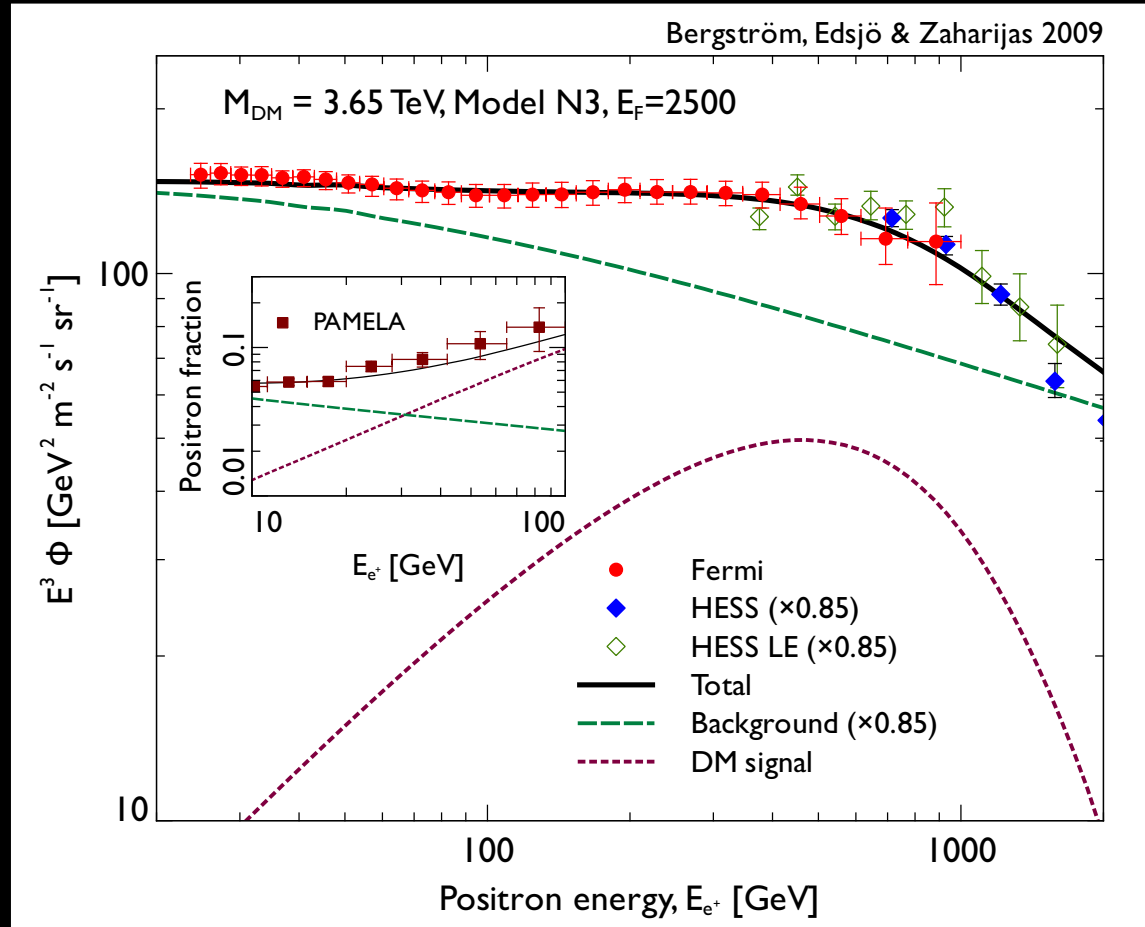
*First observational evidence
Ackermann et al 2013*

- Secondary cosmic rays (^2H , ^3He , $^{6,7}\text{Li}$, $^{7,9,10}\text{Be}$, $^{10,11}\text{B}$, ..., ^{26}Al , ^{35}Cl , ^{54}Mn , ...) are produced in cosmic ray collisions with the interstellar medium (90% H, 10% He).
- Secondary to primary ratio carries information on astrophysical model.



Background graphics from Moskalenko 2005

Excess in cosmic ray positrons



Nomura-Thaler model:

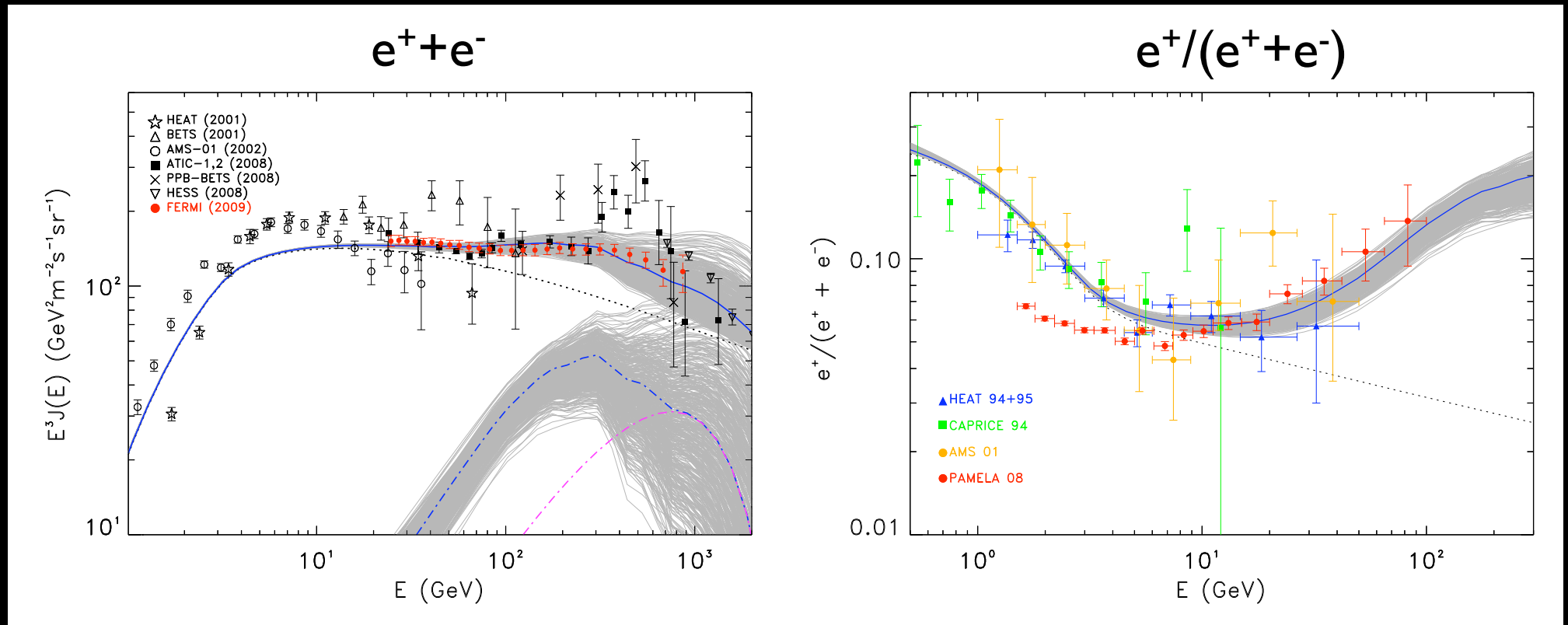
Bergstrom, Edsjo, Zaharijas 2009

$$DM + DM \rightarrow s + a, \quad s \rightarrow a + a, \quad a \rightarrow \mu^+ \mu^-$$

$$m_s = 20 \text{ GeV} \quad m_a = 0.5 \text{ GeV}$$

Excess in cosmic ray positrons

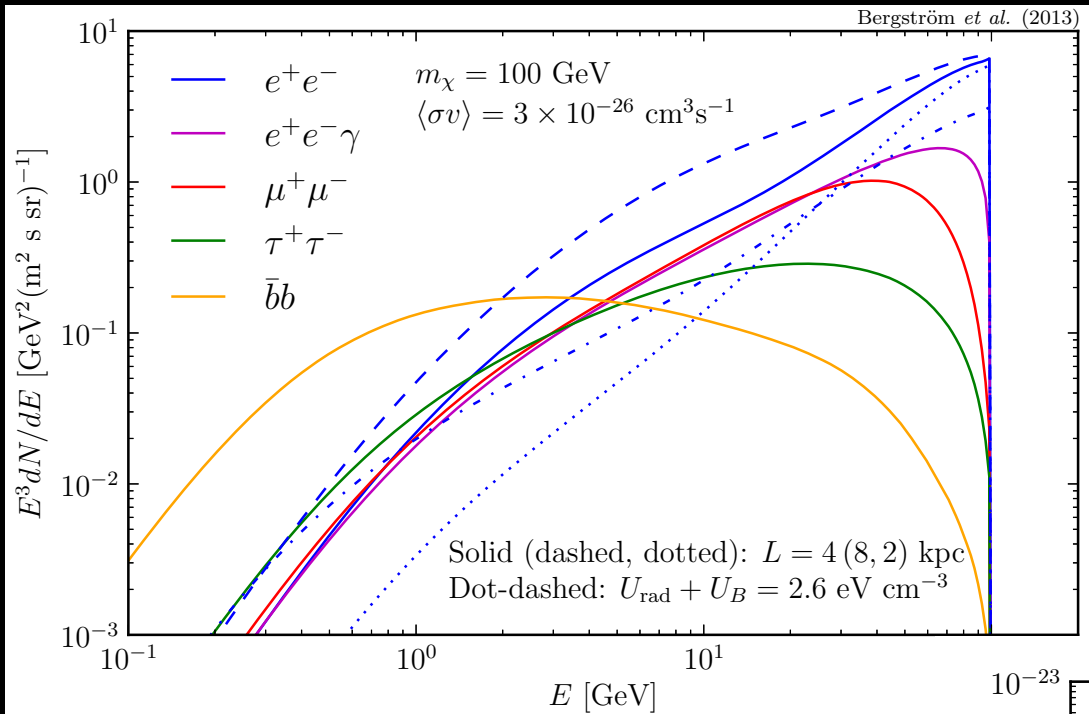
Pulsars



Grasso et al [Fermi-LAT], arXiv: 0905.0636

Many parameters and models to choose from.

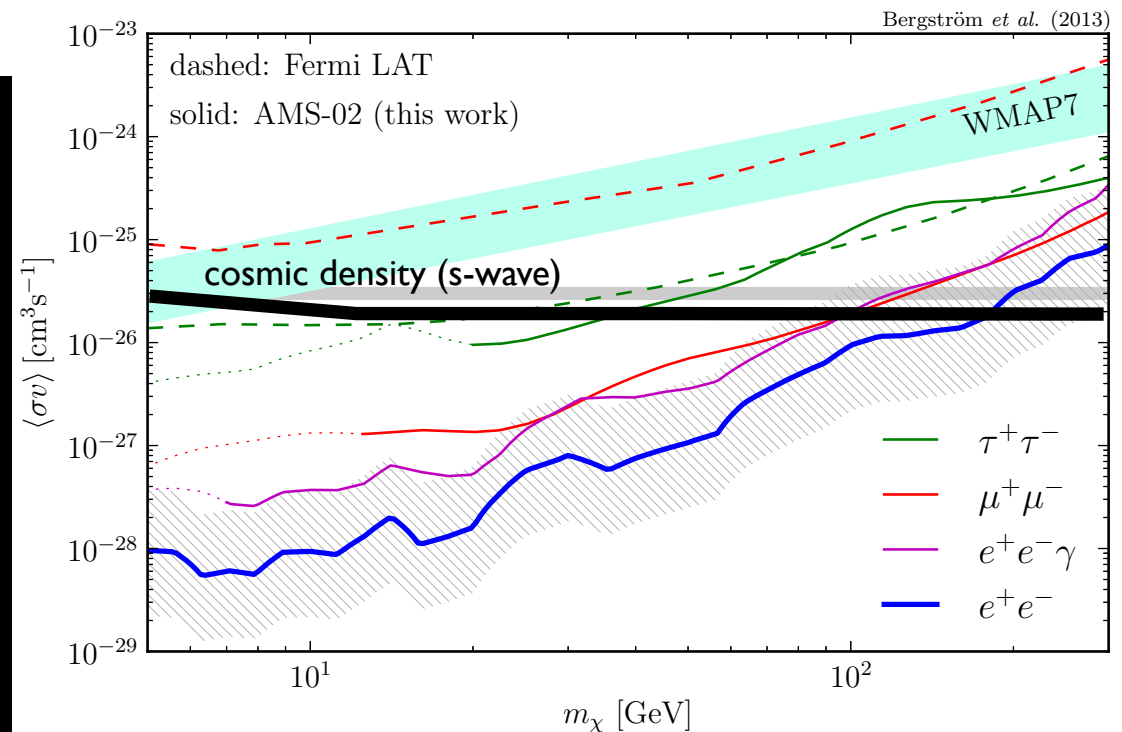
Excess in cosmic ray positrons



The safe way: use the AMS spectrum purely as upper limit on positrons from WIMP dark matter.

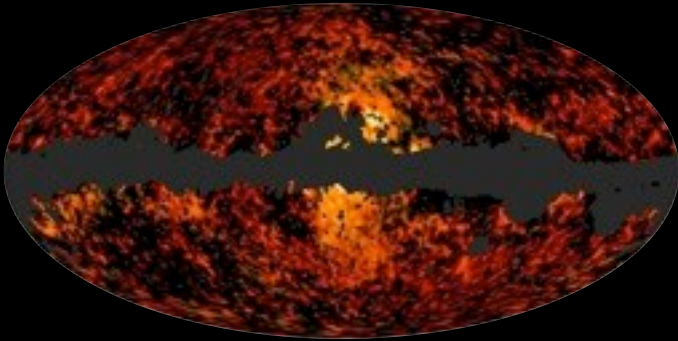
Bergstrom *et al* 2013

Spectral features in e^+e^- spectrum lead to limits on annihilation cross section



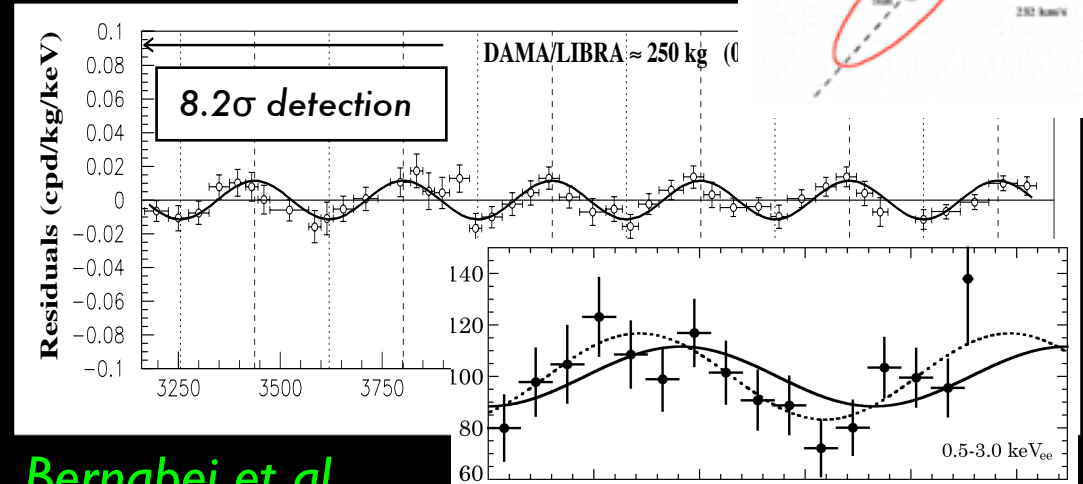
Evidence for cold dark matter particles?

WMAP/Planck haze



Annual modulation

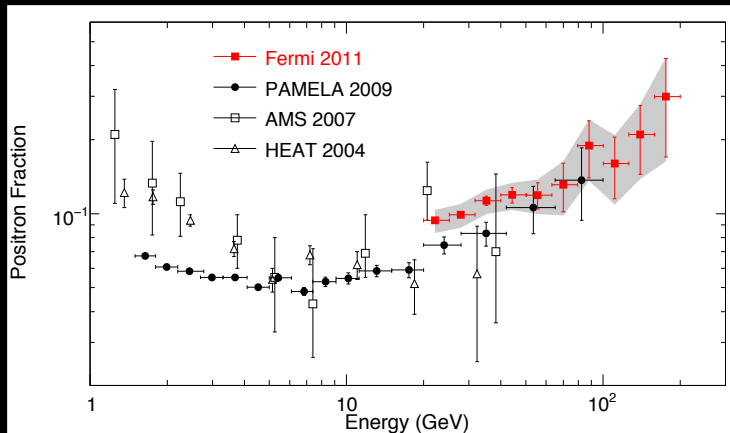
Drukier, Freese, Spergel 1986



*Bernabei et al
1997-2012*

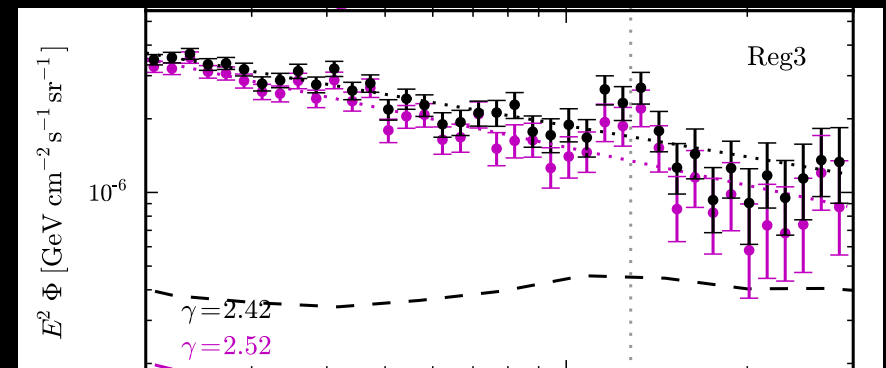
Aalseth et al 2011

Positron excess



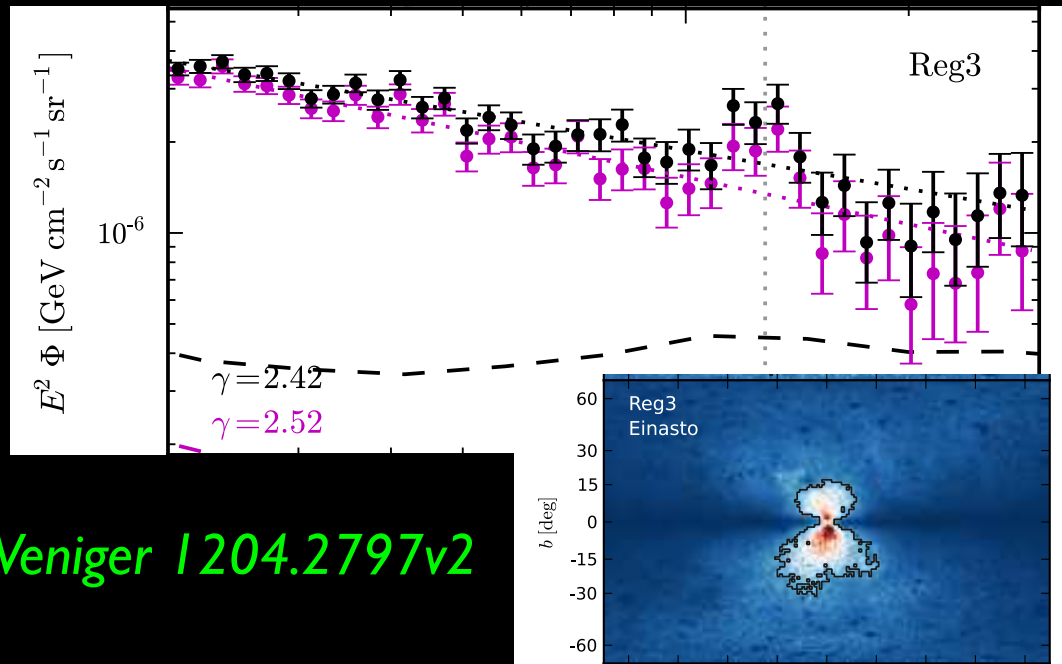
Adriani et al 2009; Ackerman et al 2011

130 GeV γ -ray line



Weniger 2012

135 GeV gamma-ray line?



Weniger 1204.2797v2

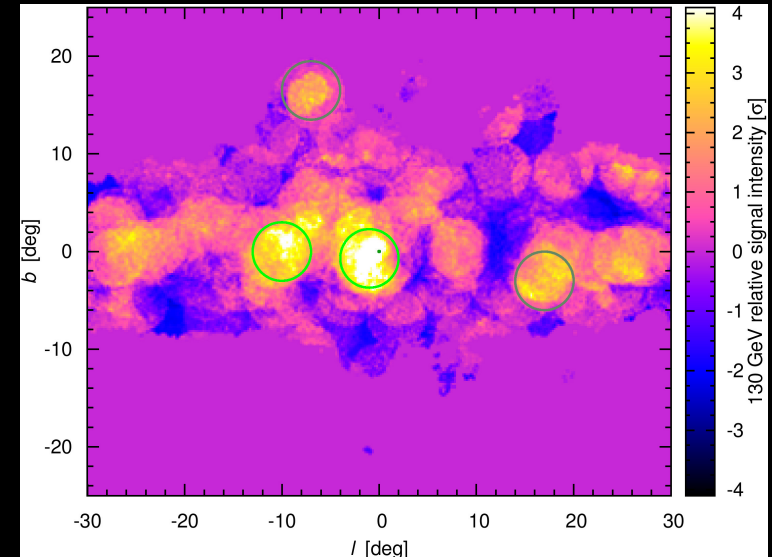
3.2 σ effect based on 50 photons

$$m = 129.8 \pm 2.4_{-13}^{+7} \text{ GeV}$$

$$\langle \sigma v \rangle_{\gamma\gamma} = (1.27 \pm 0.32_{-0.28}^{+0.18}) \times 10^{-27} \text{ cm}^3 \text{s}^{-1}$$

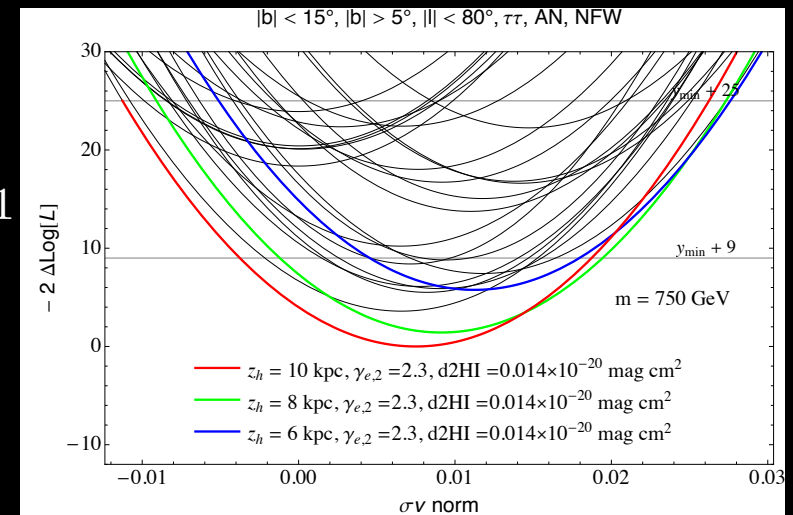
HESS-2 will tell (July 2013?)

found by others



Tempel, Hektor, Raidal 2012

Fermi Collab. upper bounds

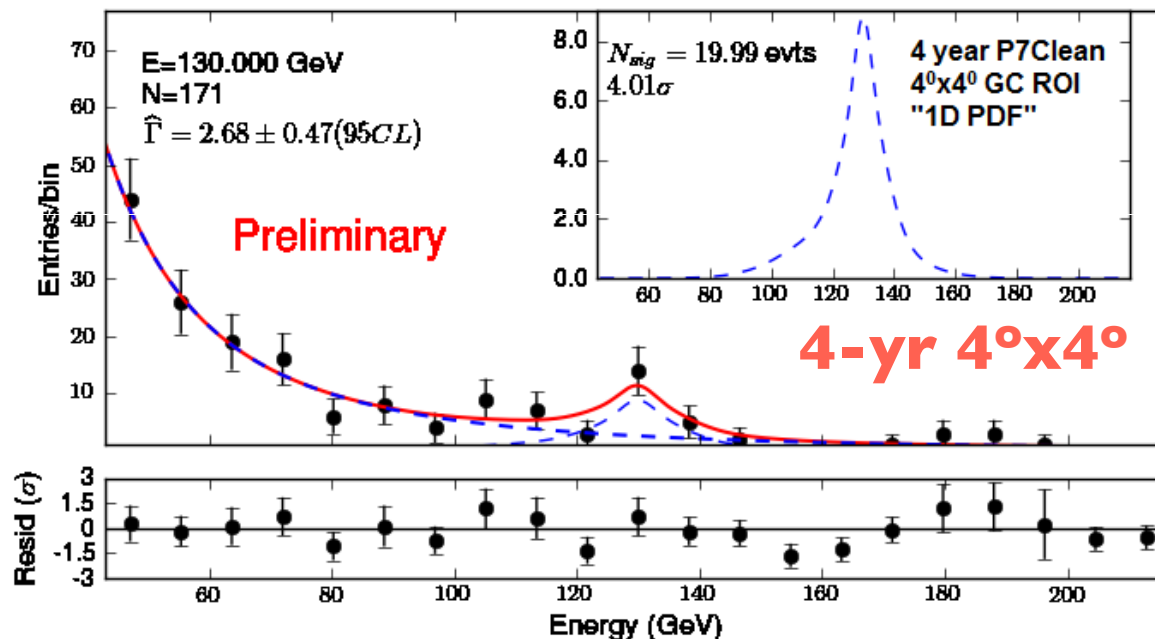
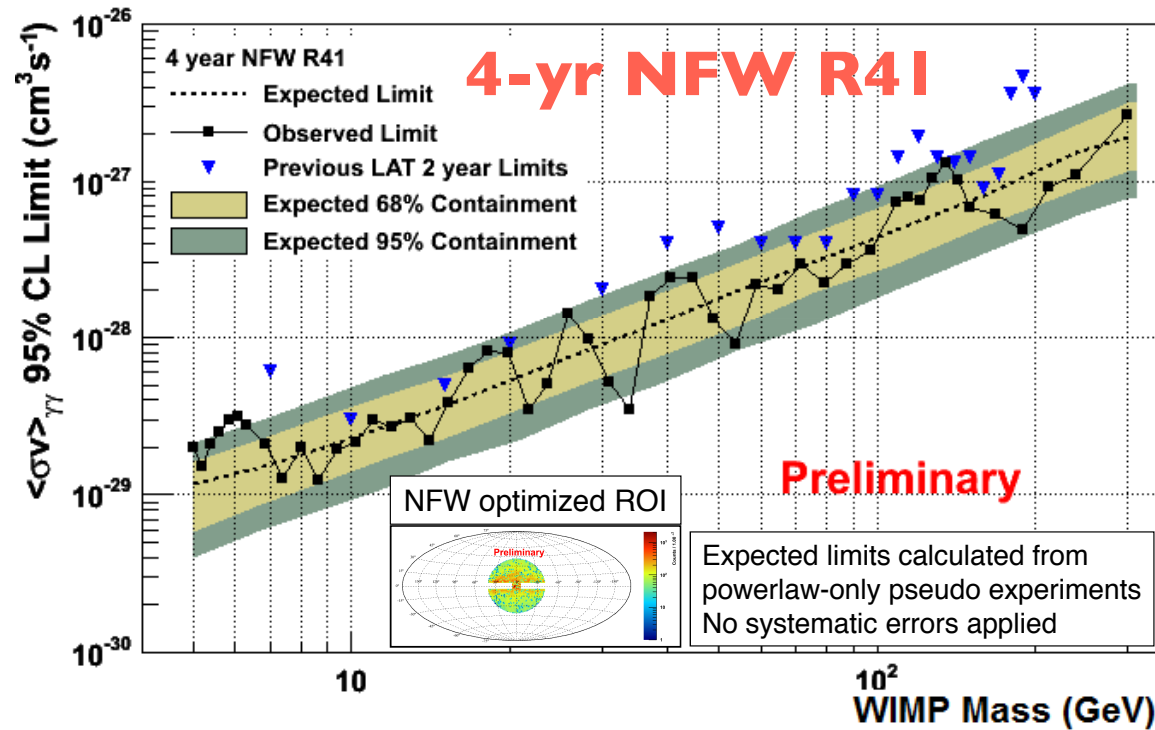


Ackerman et al (Fermi-LAT) 2012

135 GeV gamma-ray line?

Bloom et al
(Fermi-LAT)
2012

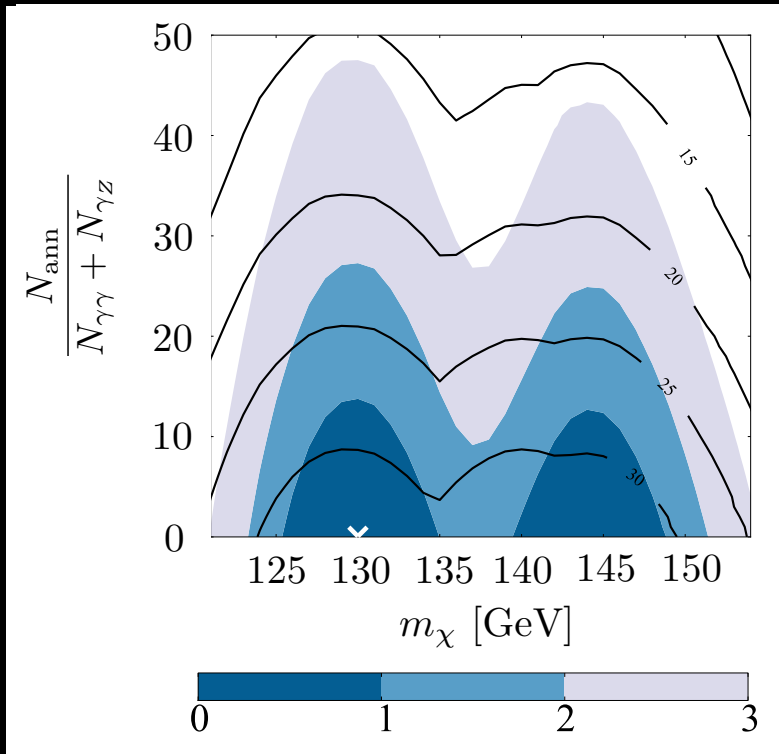
Albert et al
(Fermi-LAT)
2012



135 GeV gamma-ray line?

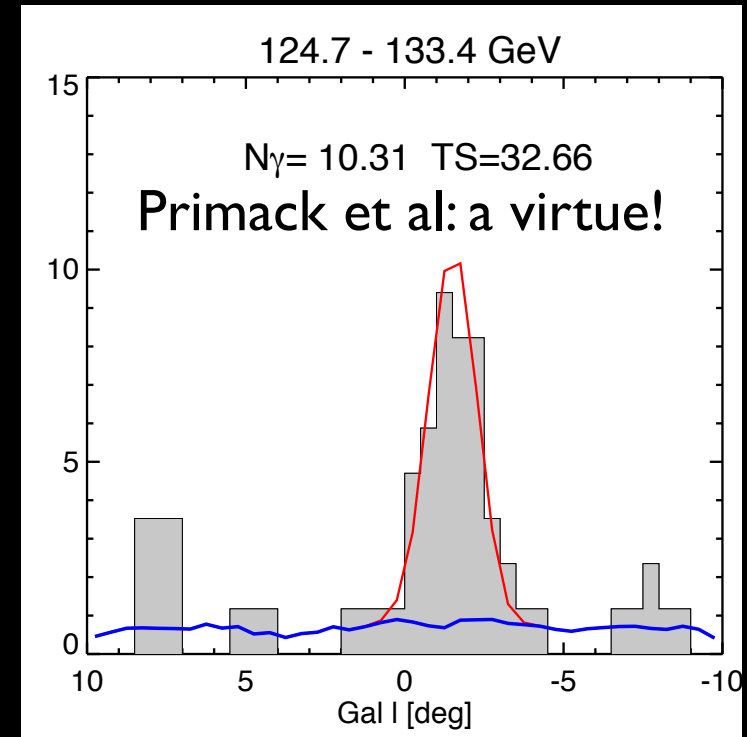
Difficulties.....

suppressed continuum

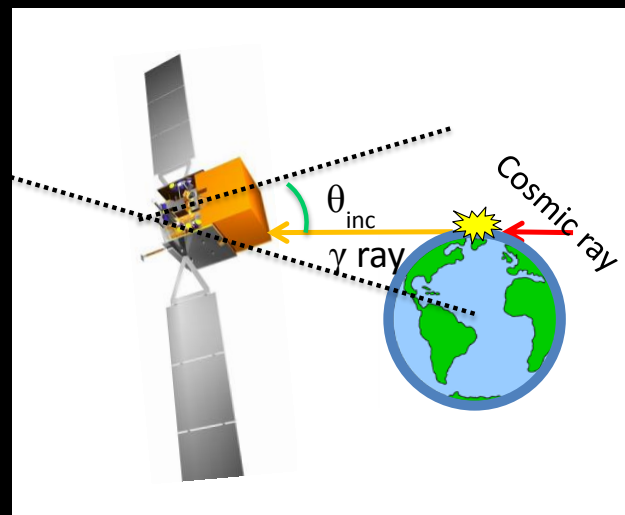


Cohen, Lisanti, Slatyer, Wacker 2012

off from Galactic Center



Su, Finkbeiner 2012



Earth limb data
set shows pile-up
at 130 GeV

135 GeV gamma-ray line: astrophysics

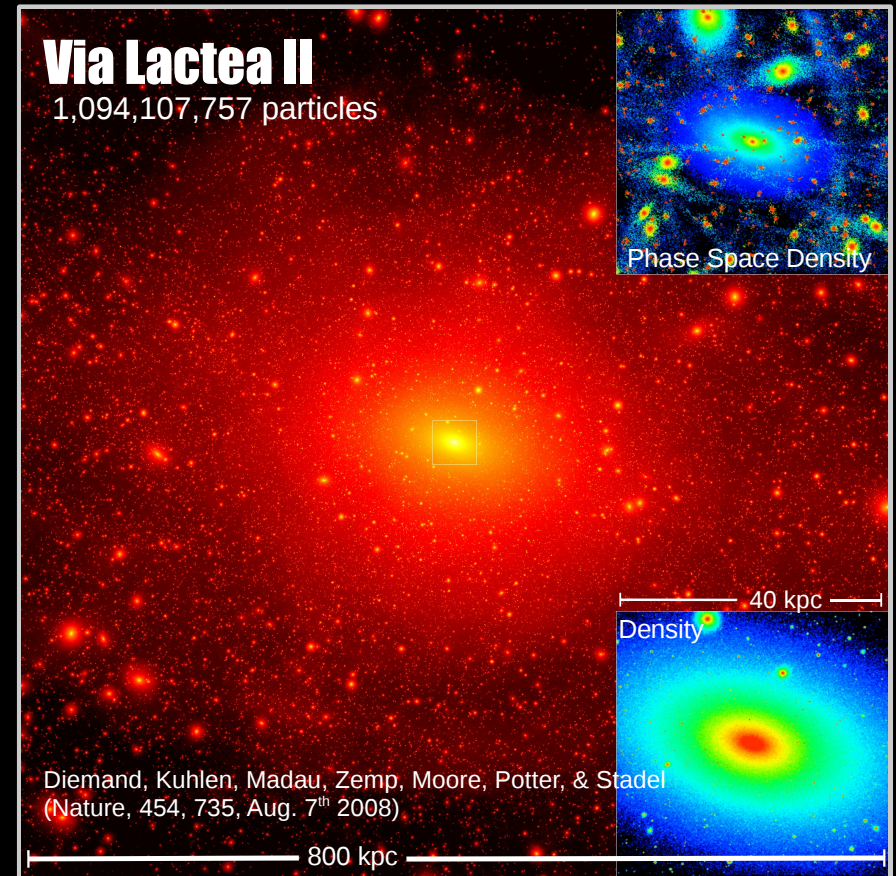
Intensity depends on halo clumpiness

Dark matter clumps, clouds, subhalos,
minihalos, microhalos, nanohalos,

$$\frac{d\Phi_\gamma}{dE} = \frac{\sigma v}{2m^2} \int \rho^2(\ell) \frac{dN_\gamma}{dE} d\ell$$

Boost factor

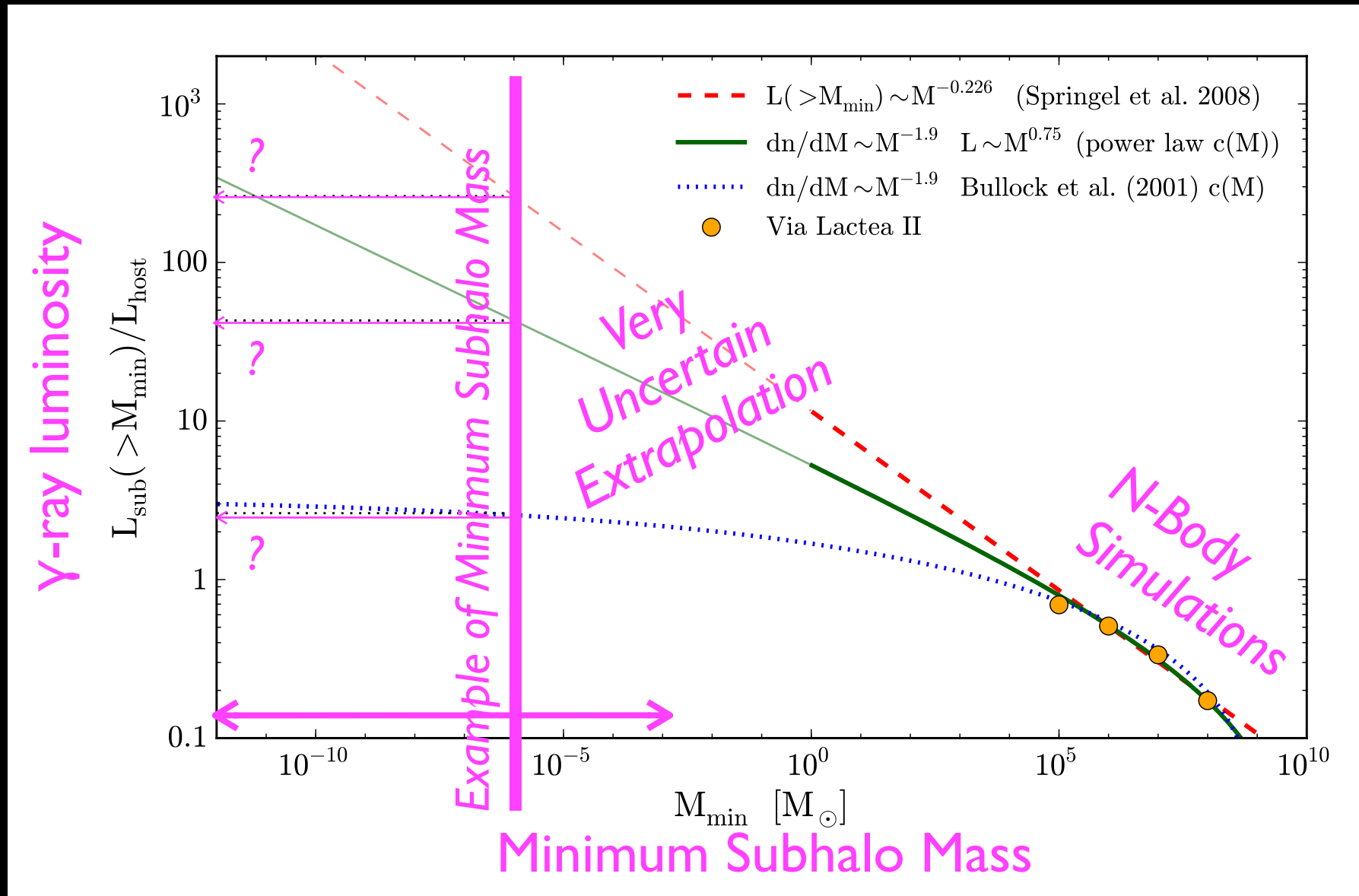
$$B = \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \quad \text{depends on position and on statistics (shape, mass) of subhalos}$$



Not just for γ -rays: positrons, antiprotons, synchrotron, etc.

135 GeV gamma-ray line: astrophysics

How small are cold dark matter halos?

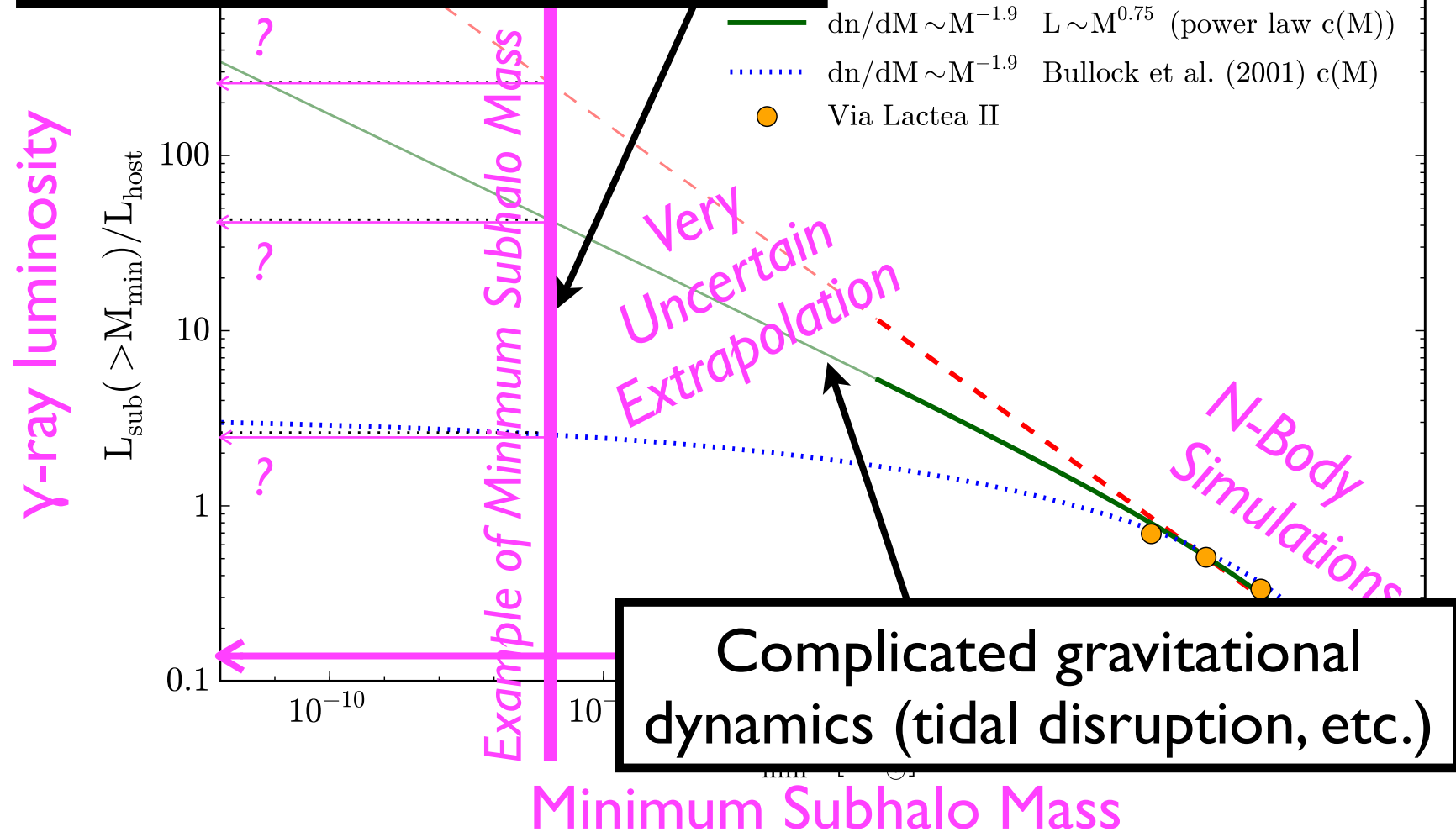


From Kuhlen, Vogelsberger, Angulo 2012

135 GeV gamma-ray line: astrophysics

How small are cold dark matter halos?

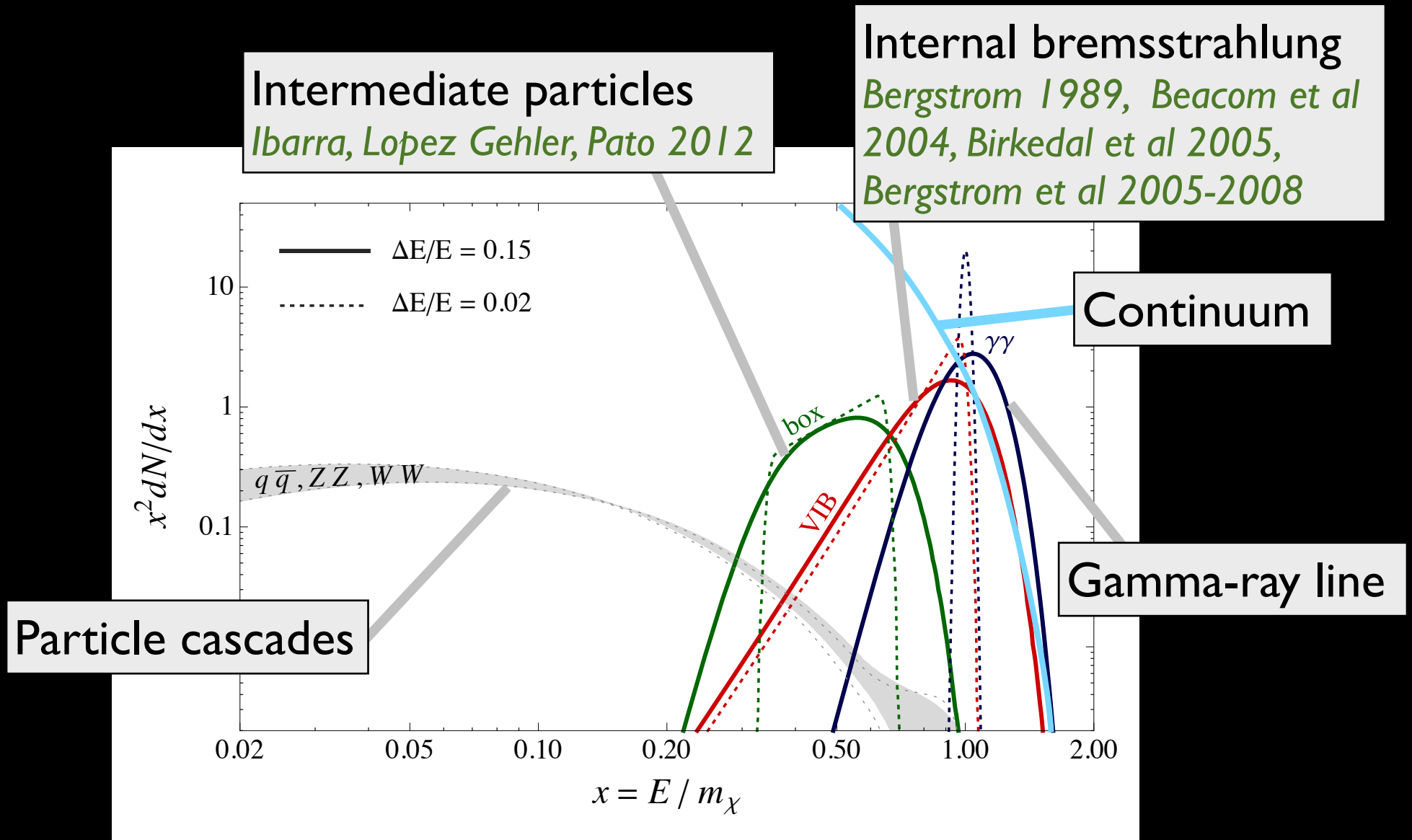
Set by time of last scattering
with plasma (particle physics)



From Kuhlen, Vogelsberger, Angulo 2012

135 GeV gamma-ray line: particle physics

Gamma-line chaperones



Bringman, Weniger 2012

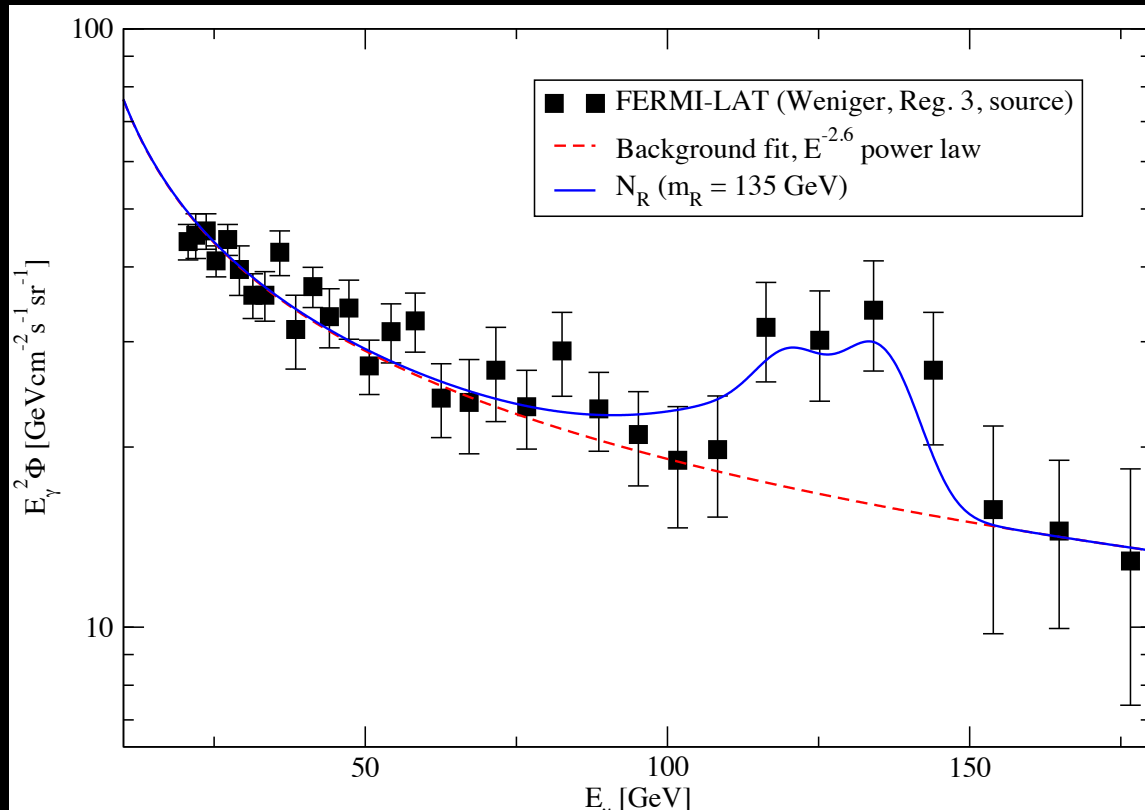
135 GeV gamma-ray line: particle physics

Highly incomplete list of suggested particle models

Models		References
S U S Y	MSSM neutralino	Acharya, Kane, Kumar, Lu, Zheng 1205.5789
	beyond-MSSM neutralino	Das, Ellwanger, Mitropoulos 1206.2639
	sneutrino	Choi, Seto 1205.3276
decaying dark matter		Kyee, Park 1205.4151; Buchmuller, Garny 1206.7056
Extended Higgs sector		Cline 1205.2688; Lee, Park, Park 1205.4675; Buckley, Hooper 1205.6811
Minimalist dark matter		Cheung, Tsai, Tseng, Yuan, Zee 1207.4930
Extra $U(1)'$		Dudas, Mambrini, Pokorski, Romagnoni 1205.1520
Kinetically-mixed $U(1)'$		Park, Park 1207.4981
Dipole dark matter		Weiner, Yavin 1206.2910; Heo, Kim 1207.1341; Cline, Moore, Frey 1208.2685
Non-SUSY GUT		Li, Maxin, Nanopoulos, Walker 1208.1999
Leptonic dark matter		Baltz, Bergstrom 2002; Bergstrom 1208.6082
.....		

135 GeV gamma-ray line: particle physics

Leptonically-Interacting Massive Particles (LIMPs)



*Baltz, Bergstrom 2002;
Bergstrom 1208.6082*

LIMPs predicted a
gamma-ray line
without a continuum

$$\mathcal{L}_{Zee} = f_{\alpha\beta} L_{\alpha}^T C i\tau_2 L_{\beta} S^+ + \mu \Phi_1^T i\tau_2 \Phi_2 S^- + \text{h.c.}$$

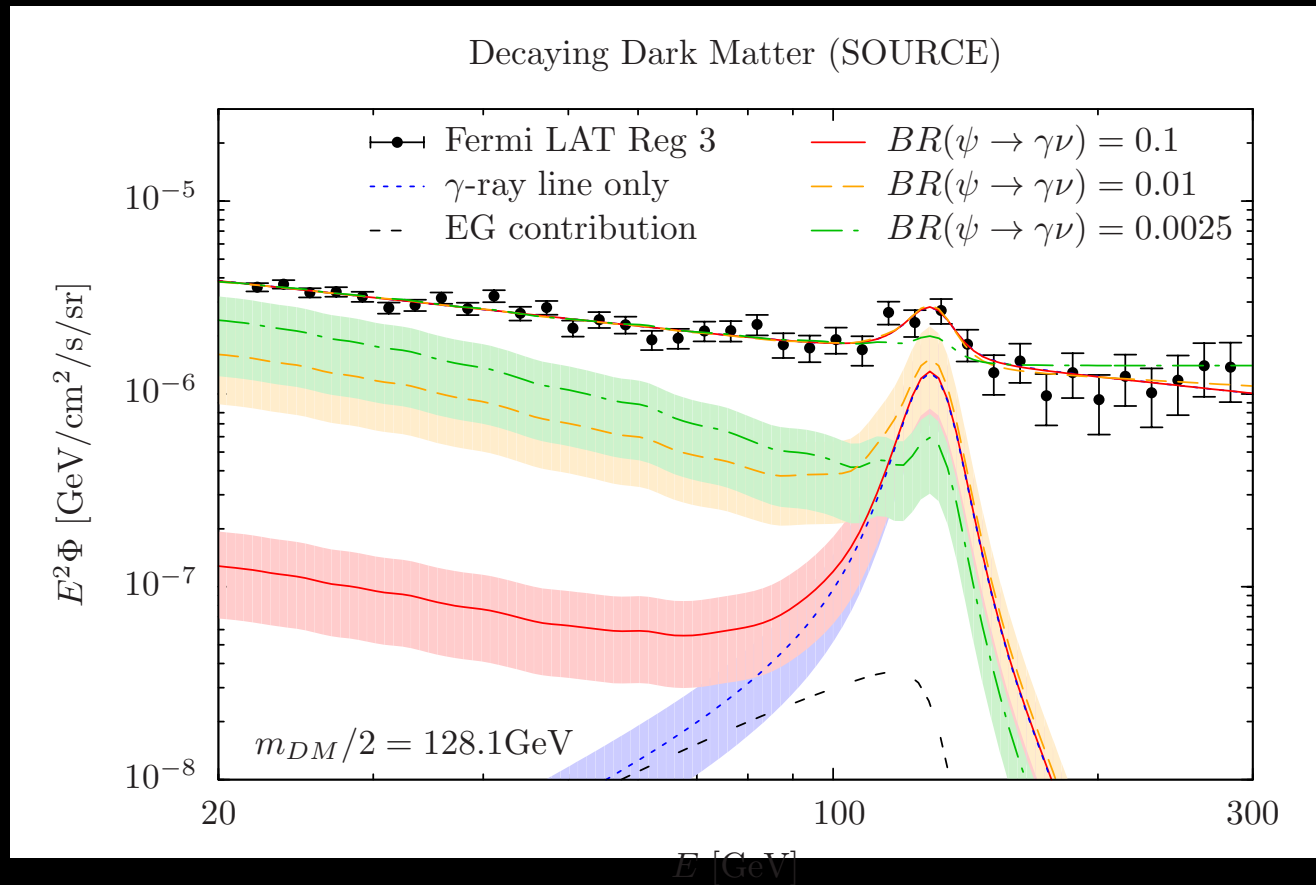
Zee 1980

$$\begin{aligned} \mathcal{L}_{\text{KNT}} = & f_{\alpha\beta} L_{\alpha}^T C i\tau_2 L_{\beta} S_1^+ + g_{\alpha} N_R S_2^+ l_{\alpha R} \\ & + M_R N_R^T C N_R + V(S_1, S_2) + \text{h.c.} , \end{aligned}$$

Krauss, Nasri, Trodden 2002

270 GeV decaying dark matter?

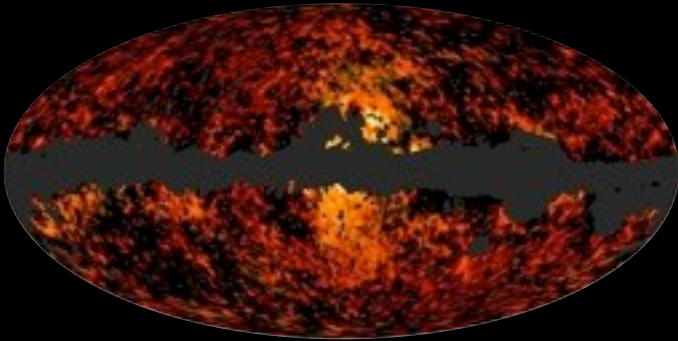
Kyae, Park *1205.4151*; Buchmuller, Garny *1206.7056*



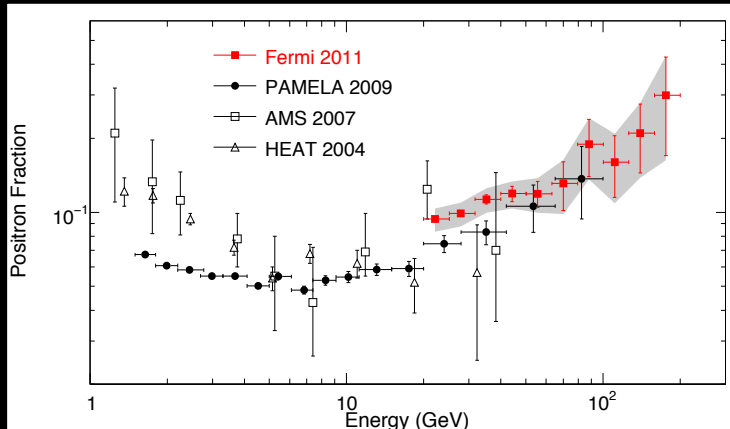
Buchmuller, Garny *1206.7056*

Evidence for cold dark matter particles?

WMAP/Planck haze



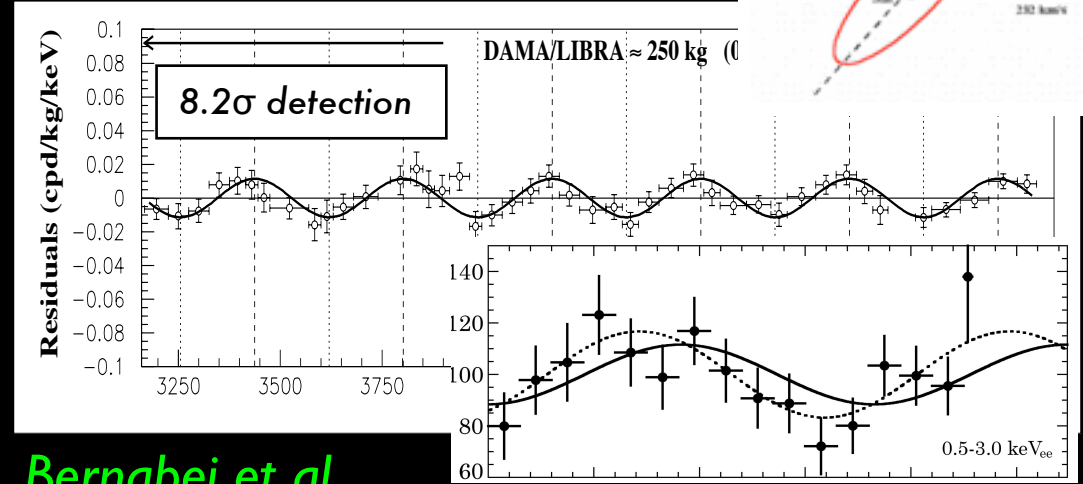
Positron excess



Adriani et al 2009; Ackerman et al 2011; Aguilar et al 2013

Annual modulation

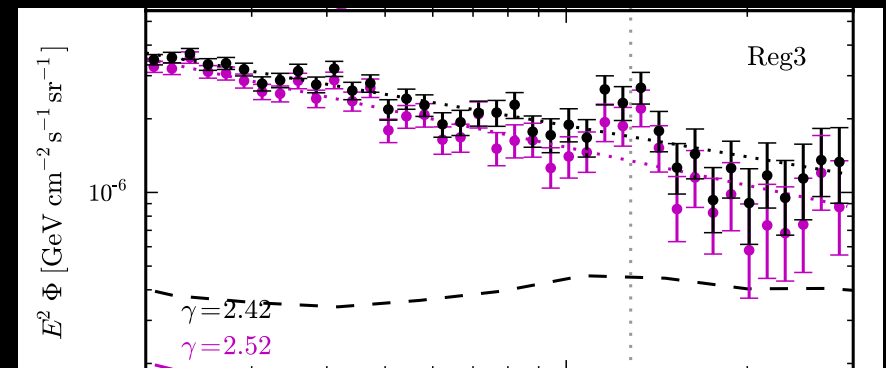
Drukier, Freese, Spergel 1986



Bernabei et al 1997-2012

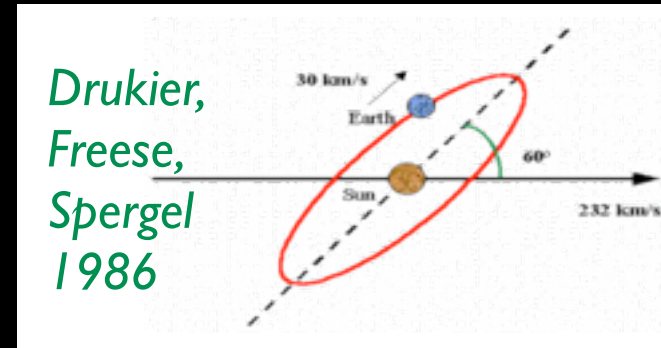
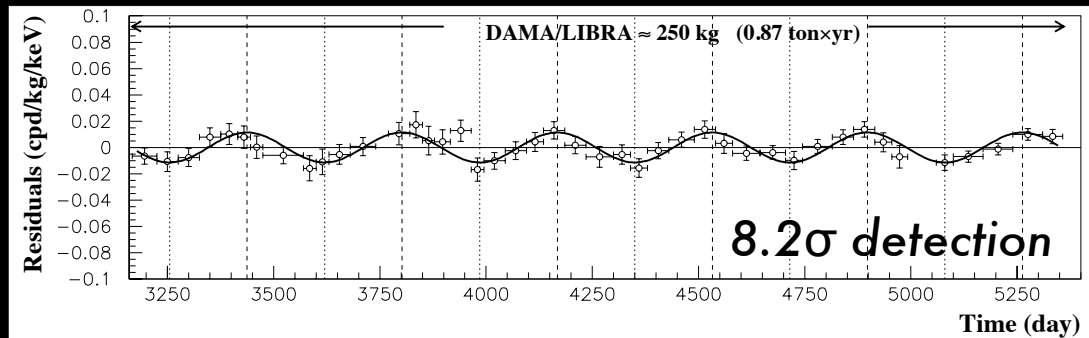
Aalseth et al 2011

130 GeV γ -ray line

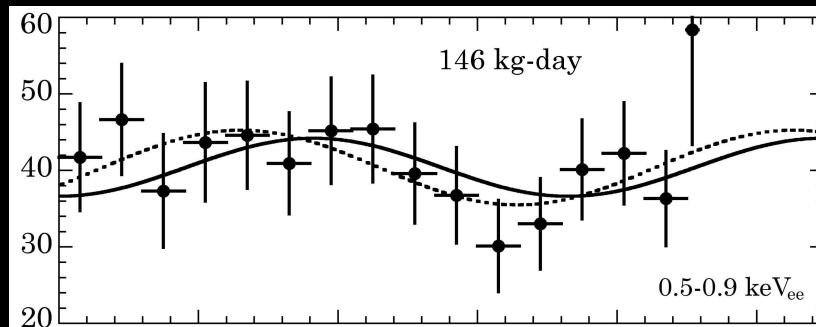


Weniger 2012

Evidence for light dark matter particles?



Bernabei et al (DAMA) 1997-10



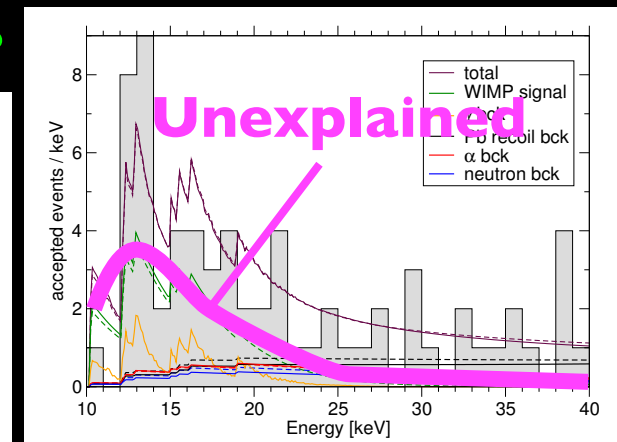
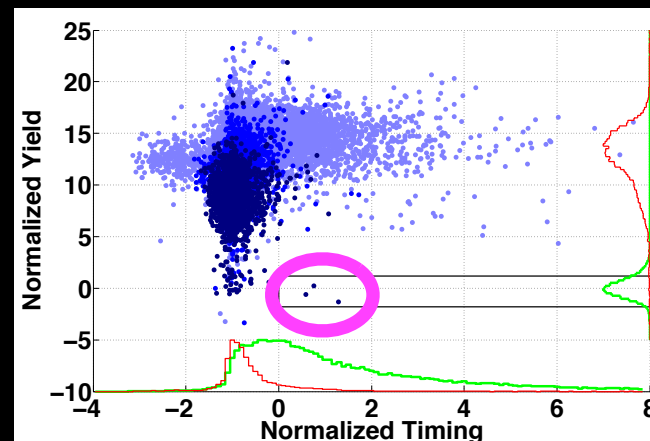
Caveat: "Rates look flatter on second year." Collar, IDM2012

Annually modulated....

Aalseth et al (CoGeNT) 1106.0650

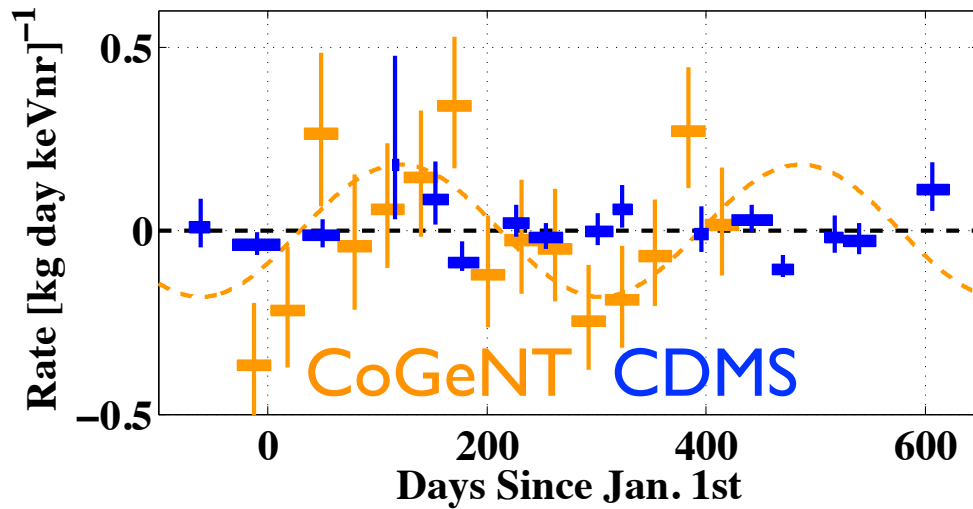
.....and unmodulated

Agnese et al (CDMS) 2013



Anglehor et al (CRESST) 2011

Evidence for light dark matter particles?



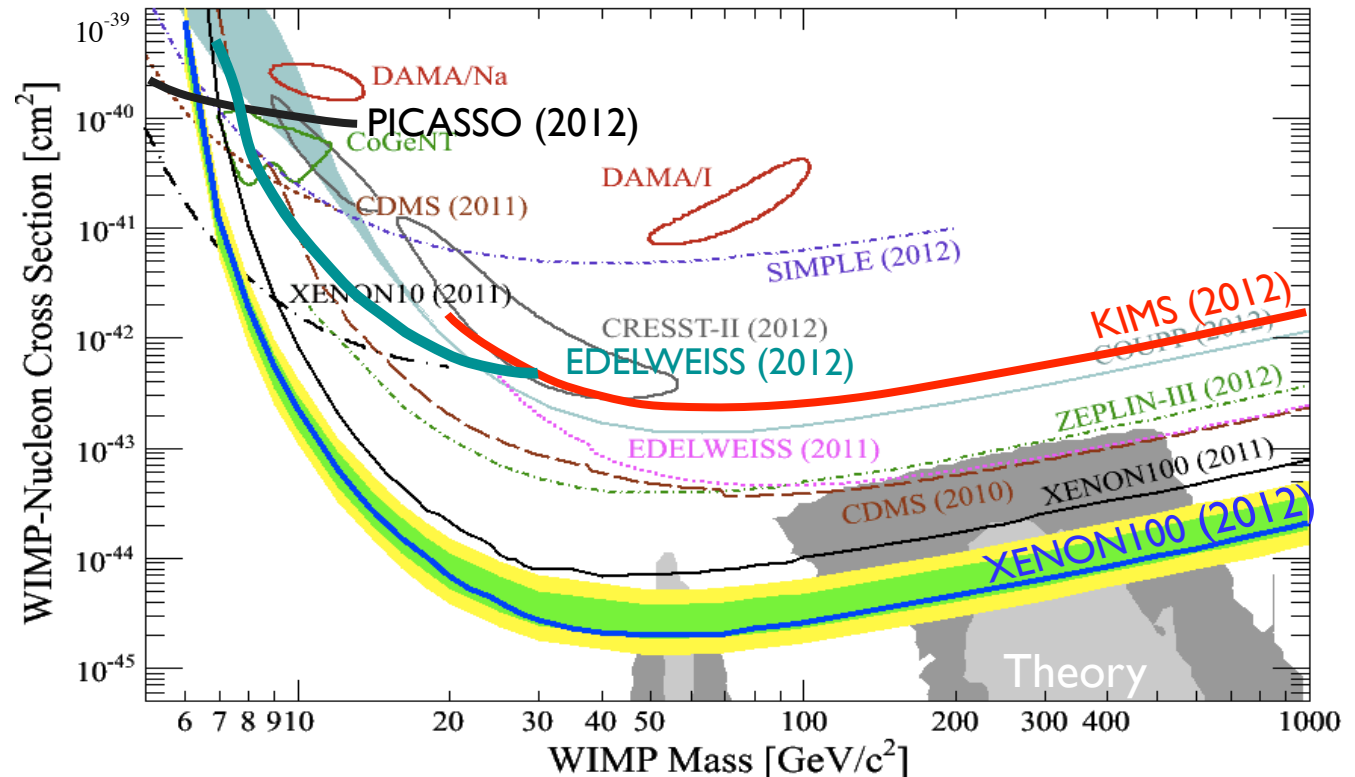
No significant modulation

Same target material

Ahmed et al (CDMS)
1203.1309

Not so many events

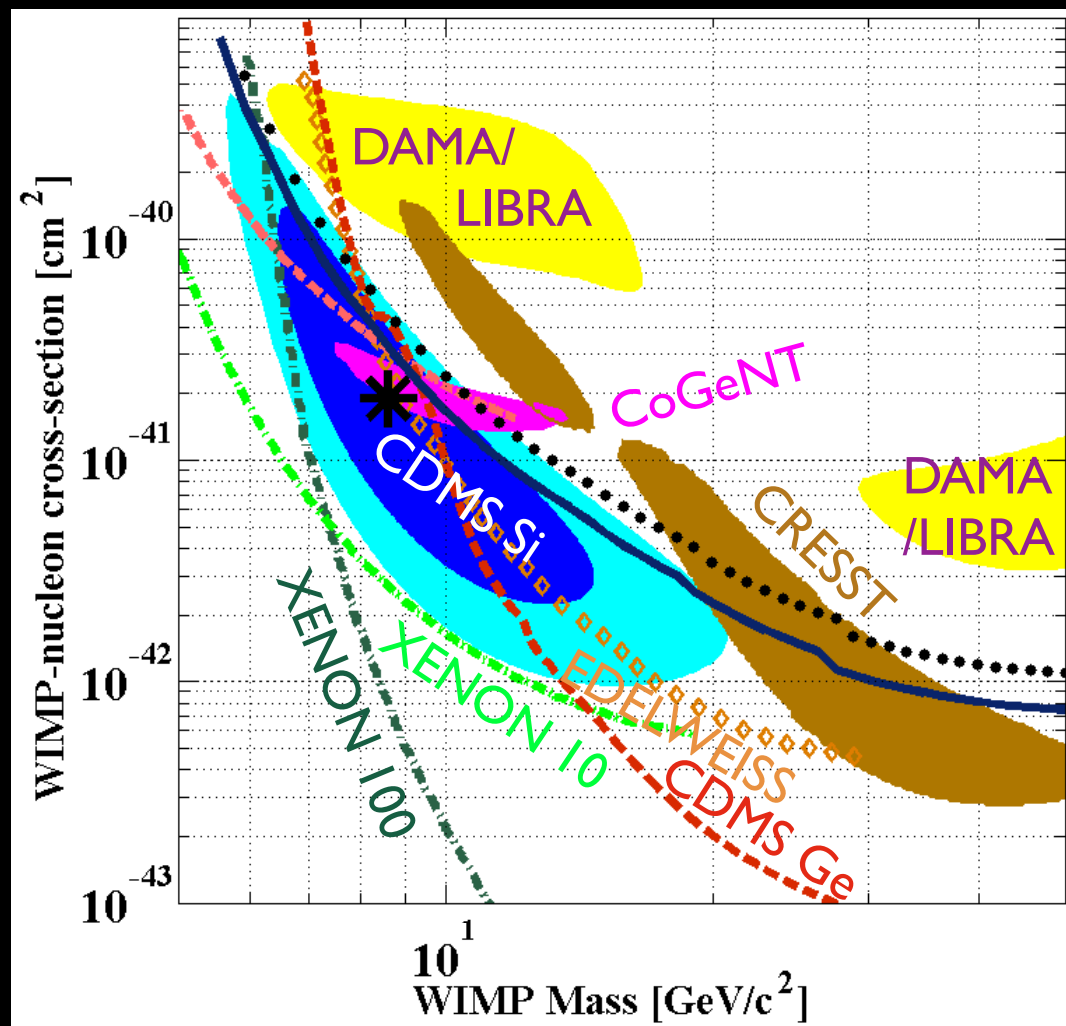
Adapted from Aprile et al (XENON-100) 2012



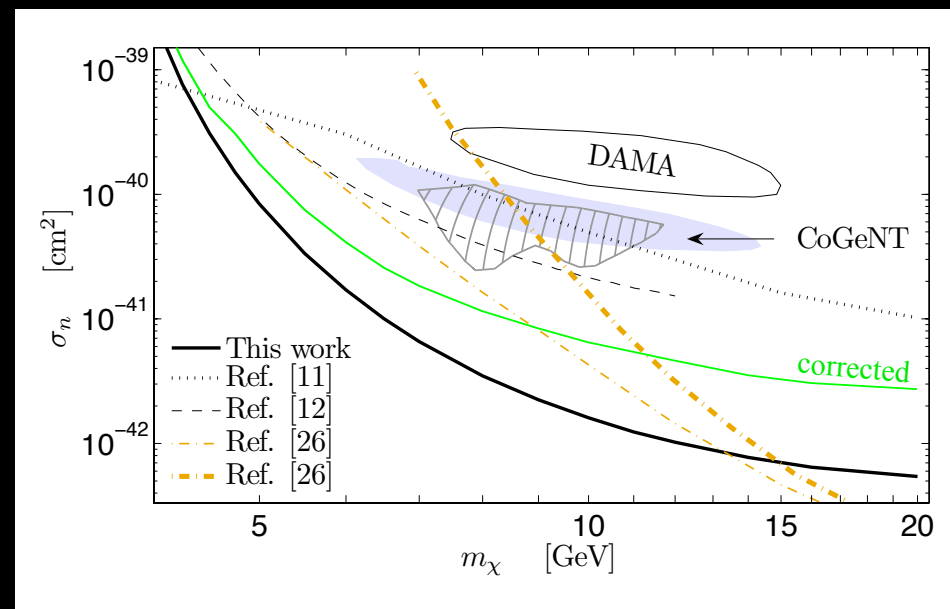
Evidence for light dark matter particles?

Angle et al (XENON10) 2013

3 events in CDMS-Si



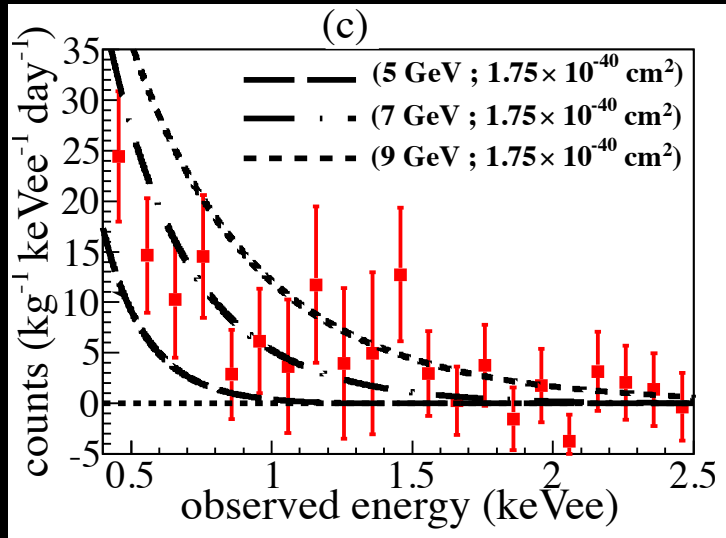
Agnese et al (CDMS) 2013



XENON10 bound weaker

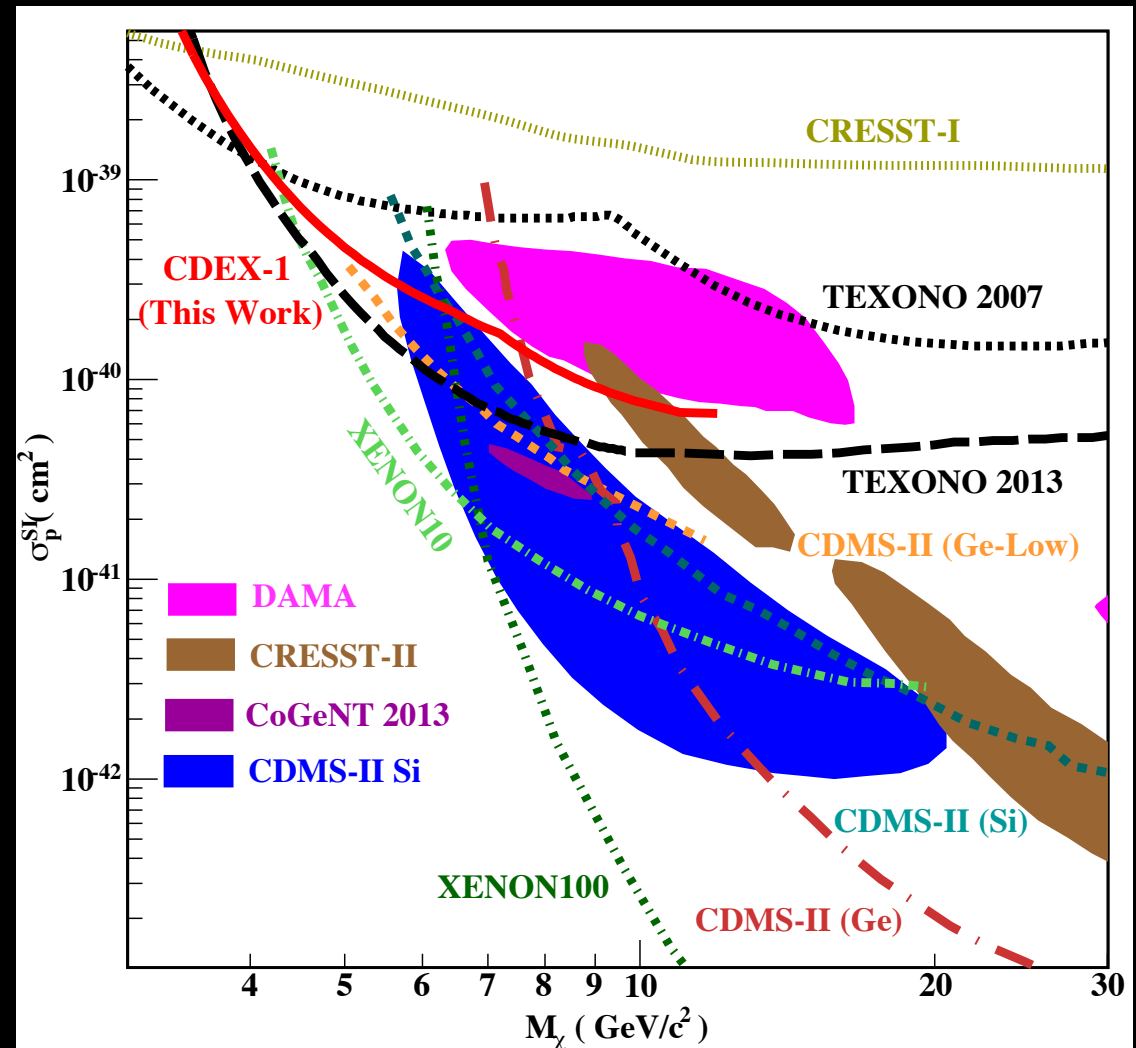
CDMS Si (2013)
CDMS Si (all)

Evidence for light dark matter particles?



No events in CDEX
(same target as
CoGeNT and
CDMS-Ge)

Zhao et al (CDEX) 2013

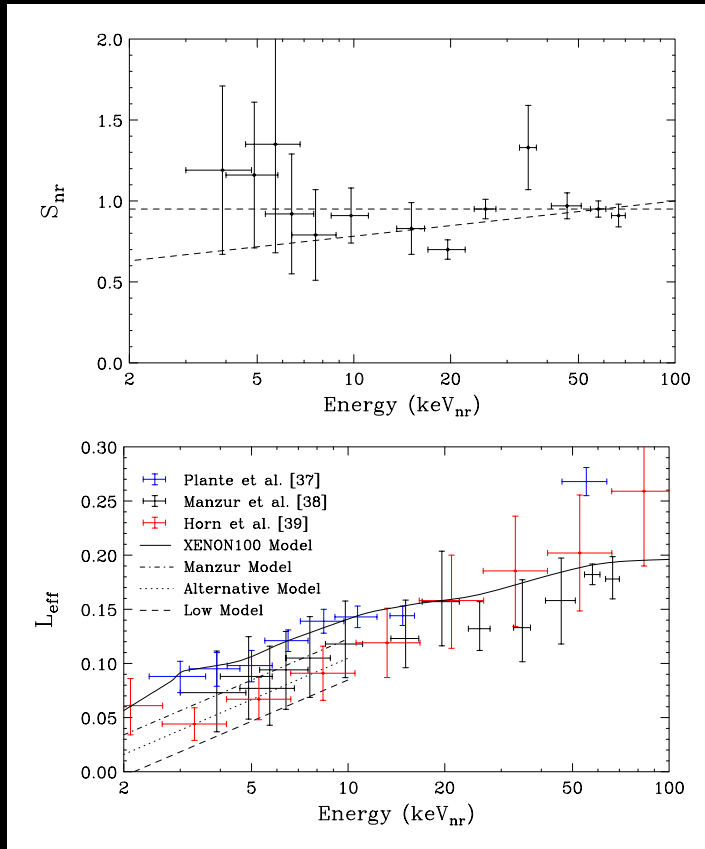


Evidence for light dark matter particles?

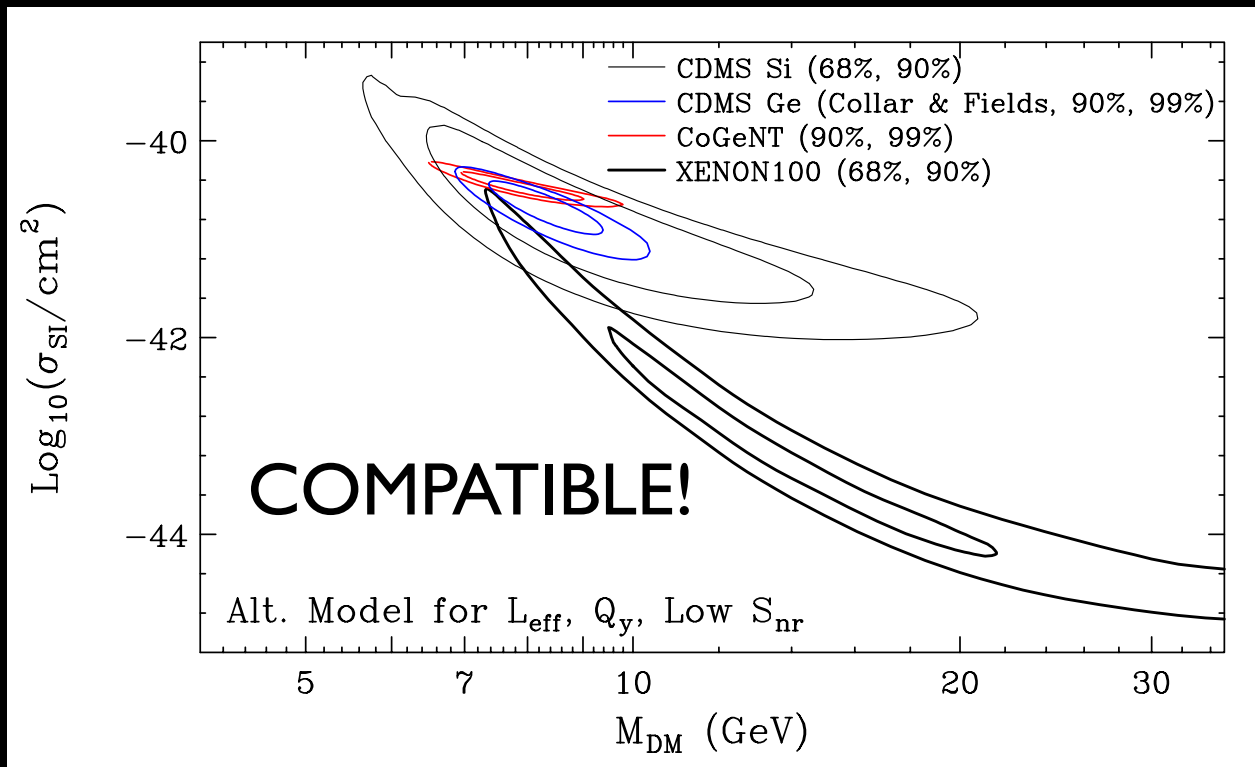
Hooper 2013

XENON100 detects events too!

Is XENON100's sensitivity overestimated?

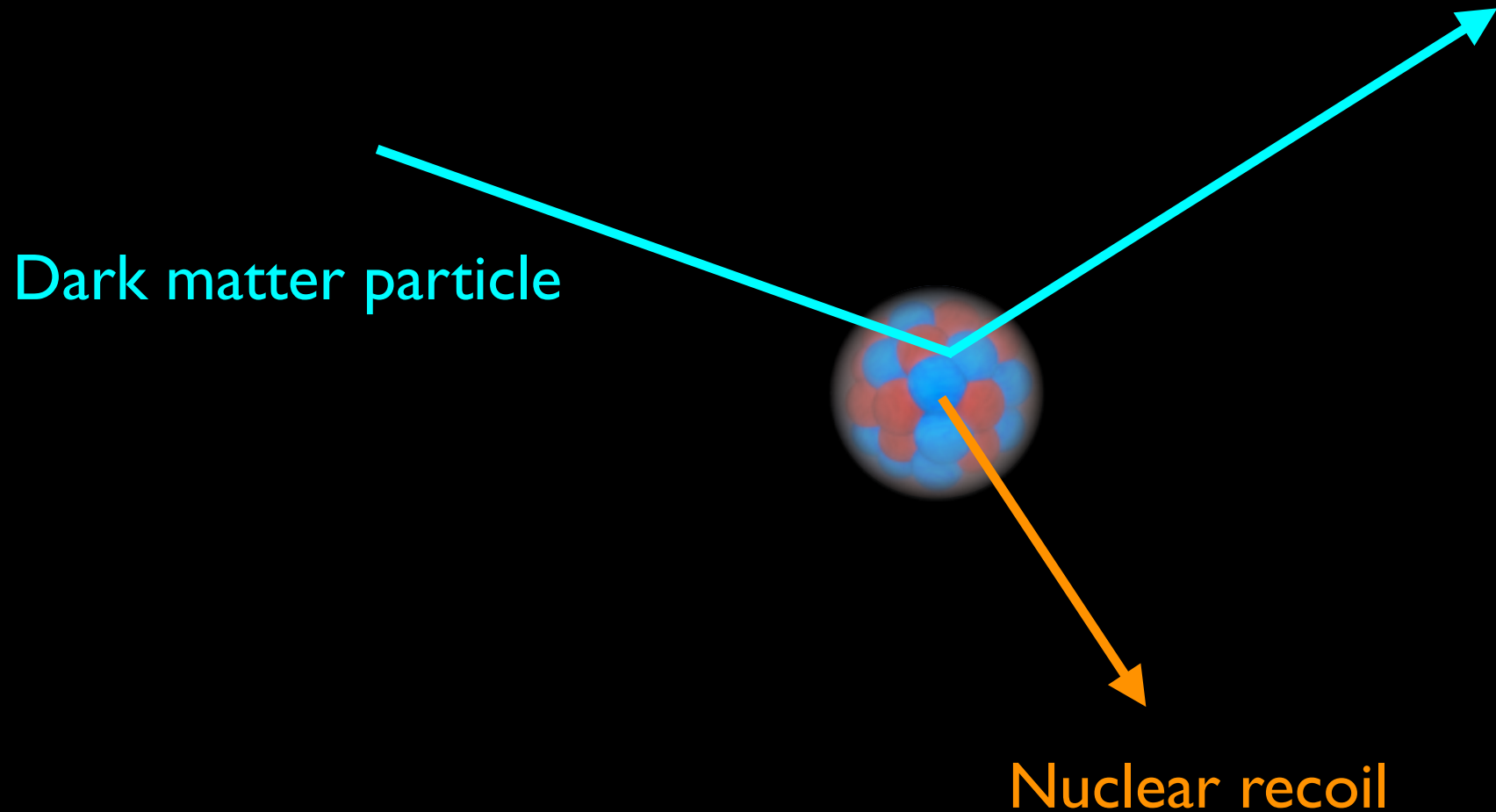


“We consider DAMA/
LIBRA and CRESST-II
more difficult to
interpret at this time”



DM-nucleus elastic scattering

$$\left(\begin{array}{c} \text{recoil} \\ \text{rate} \end{array} \right) = \left(\begin{array}{c} \text{particle} \\ \text{physics} \end{array} \right) \times (\text{astrophysics})$$



Particle physics model

$$\left(\begin{array}{c} \text{recoil} \\ \text{rate} \end{array}\right) = \boxed{\left(\begin{array}{c} \text{particle} \\ \text{physics} \end{array}\right)} \times (\text{astrophysics})$$

What force couples dark matter to nuclei?

Coupling to either nucleon number density or nucleon spin density

$$\left(\begin{array}{c} \text{particle} \\ \text{physics} \end{array}\right) = \frac{\sigma_{SI}(E) + \sigma_{SD}(E)}{2m\mu^2}$$

Spin-independent and spin-dependent cross sections

Reduced mass $\mu = mM/(m + M)$

$$\sigma(E) = E_{\max} \frac{d\sigma}{dE} = \frac{2\mu^2 v^2}{m} \frac{d\sigma}{dE}$$

Particle physics model

1-10 GeV WIMP; very incomplete

Models		References
S U S Y	MSSM neutralino	Goldberg 1983; Griest 1988; Gelmini, Gondolo, Roulet 1989; Griest, Roszkowski 1991; Bottino et al 2002-11; Kuflik, Pierce, Zurek 2010; Feldman et al 2010; Cumberbatch et al 2011; Belli et al 2011;
	beyond-MSSM neutralino	Flores, Olive, Thomas 1990; Gunion, Hooper, McElrath 2005; Belikov, Gunion, Hooper, Tait 2011; Belanger, Kraml, Lessa 1105.4878;
	sneutrino	; An, Dev, Cai, Mohapatra 1110.1366; Cerdeno, Huh, Peiro, Seto 1108.0978;
minimalist dark matter (real singlet scalar with Z_2)		Silveira, Zee 1985; Veltman, Ydnurain 1989; McDonald 1994; Burgess, Pospelov, ter Veldhuis 2000; Davoudiasl, Kitano, Li, Murayama 2004; Andreas et al 2008-10; He, Tandean 1109.1267;
technicolor and alike		; Lewis, Pica, Sannino 1109.3513;
kinetically-mixed $U(1)'$ (Higgs portal)		; Foot 2003-10; Kaplan et al 1105.2073; An, Gao 1108.3943; Fornengo, Panci, Regis 1108.4661; Andreas, Goodsell, Ringwald 1109.2869; Andreas 1110.2636; Feldman, Perez, Nath 1109.2901;
baryonic $U(1)'$		Gondolo, Ko, Omura ; Cline, Frey 1109.4639;
.....		

Particle physics model

$$\left(\begin{array}{c} \text{recoil} \\ \text{rate} \end{array}\right) = \boxed{\left(\begin{array}{c} \text{particle} \\ \text{physics} \end{array}\right)} \times (\text{astrophysics})$$

Energy and/or velocity dependent scattering cross sections

nucleus	DM	$E_{\max} d\sigma/dE$	
		light mediator	heavy mediator
“charge”	“charge”	$1/E^2$	$1/M^4$
“charge”	dipole	$1/E$	E/M^4
dipole	dipole	$\text{const} + E/v^2$	E^2/M^4

All terms may be multiplied by nuclear or DM form factors $F(E)$

See e.g. Barger, Keung, Marfatia 2010; Fornengo, Panci, Regis 2011; An et al 2011

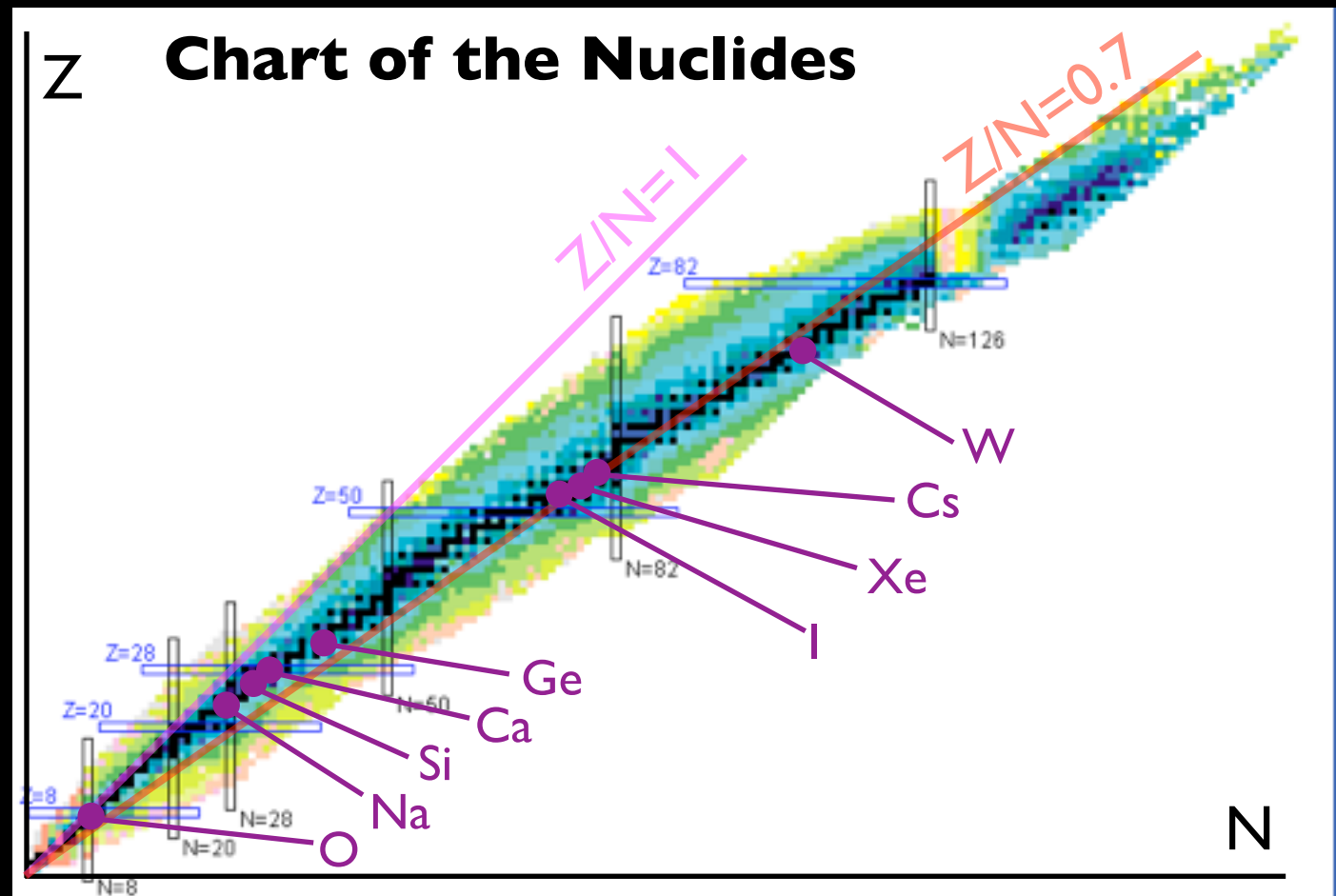
Isospin-violating dark matter

Spin-independent couplings to protons stronger than to neutrons allow modulation signals compatible with other null searches

Kurylov, Kamionkowski 2003; Giuliani 2005; Cotta et al 2009; Chang et al 2010; Kang et al 2010; Feng et al 2011; Del Nobile et al 2011;

coupling $Nf_n + Zf_p \approx 0$ for $f_n/f_p \approx -Z/N$

Why $f_n/f_p = -0.7$
suppresses the
coupling to Xe



Light neutralinos in the MSSM

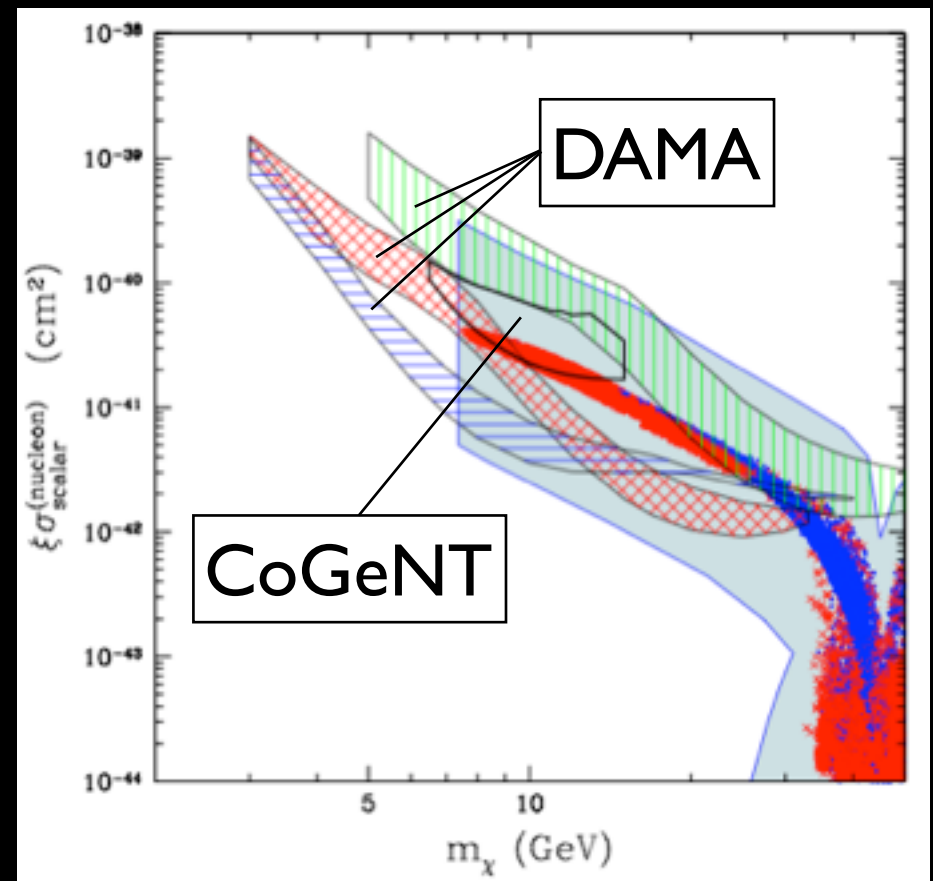
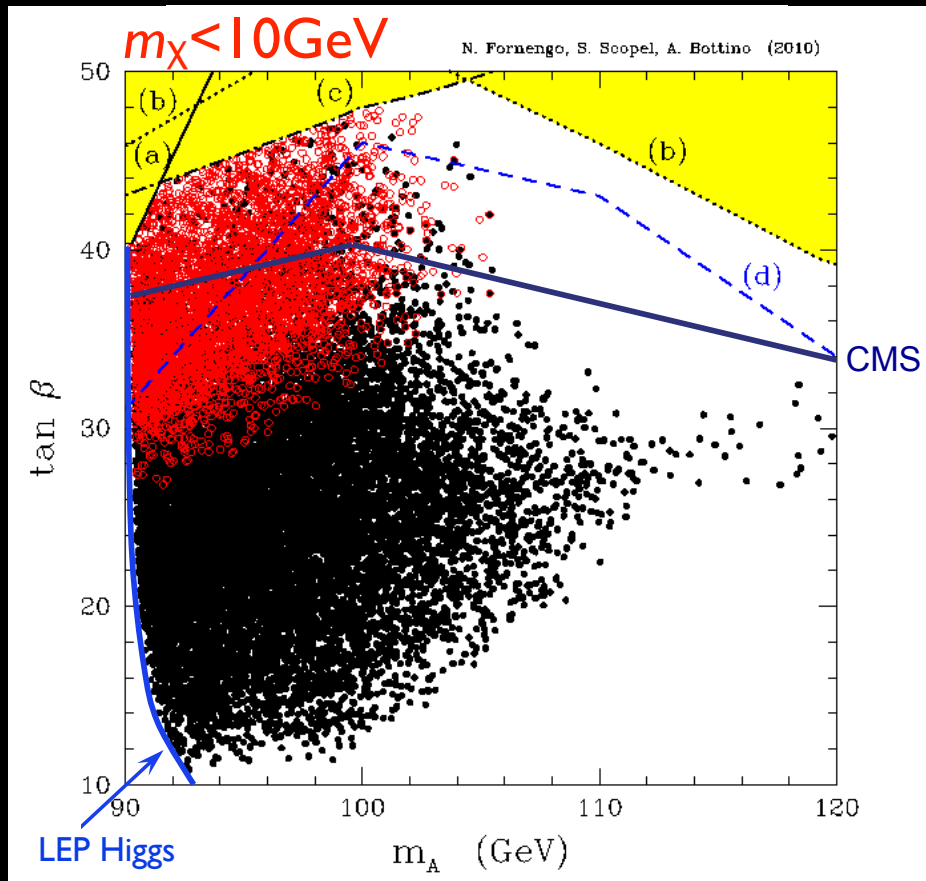
Bottino, Donato, Fornengo, Scopel 2003-2011 Non-GUT MSSM

~ 10 GeV neutralinos may account for DAMA, CoGeNT, and CRESST

“light” Higgs (~ 90 GeV) — enhanced couplings (large $\tan \beta$)

Fornengo at TAUP 2011

Belli et al 1106.4667



Light neutralinos in the MSSM

Bottino, Donato, Fornengo, Scopel 2003-2011 Non-GUT MSSM

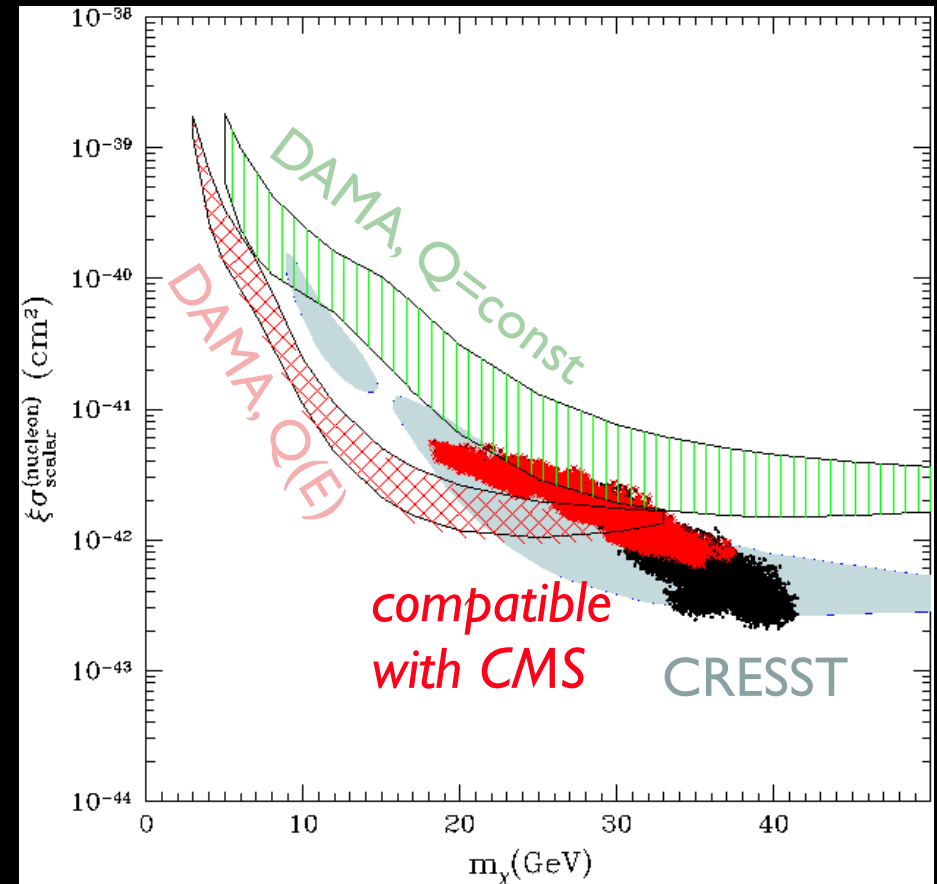
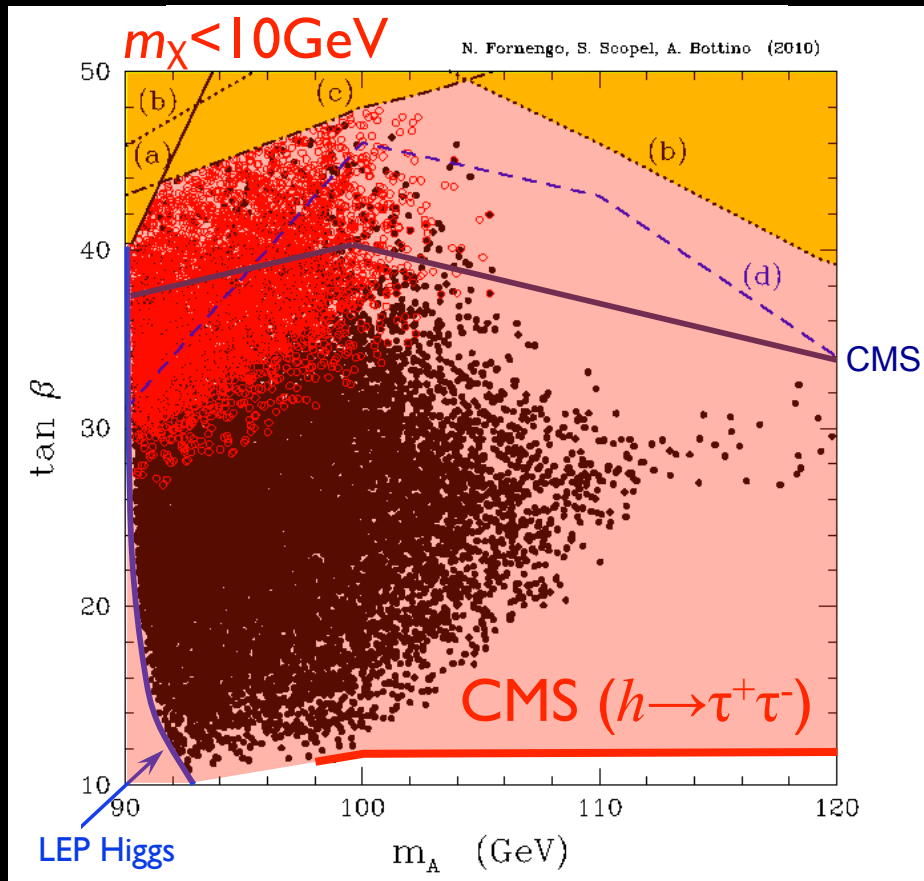
~10 GeV neutralinos may account for DAMA, Co~~X~~NT, and CRESST

negative LHC Higgs searches impose $m_\chi > 18$ GeV

(see also Kuflik, Pierce, Zurek 2010)

Fornengo at TAUP 2011

Bottino et al 1112.5666



Minimalist dark matter

do not confuse with minimal dark matter

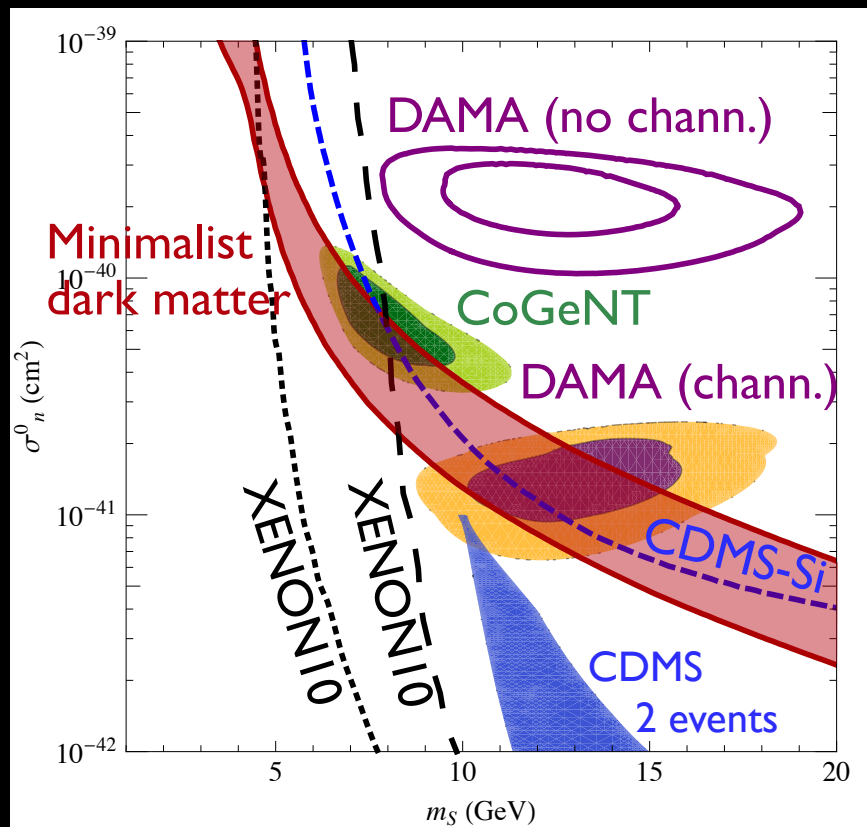
Gauge singlet scalar field S , stabilized by Z_2 symmetry

$$\mathcal{L}_S = \frac{1}{2} \partial^\mu S \partial_\mu S - \frac{1}{2} \mu_S^2 S^2 - \frac{\lambda_S}{4} S^4 - \lambda_L H^\dagger H S^2$$

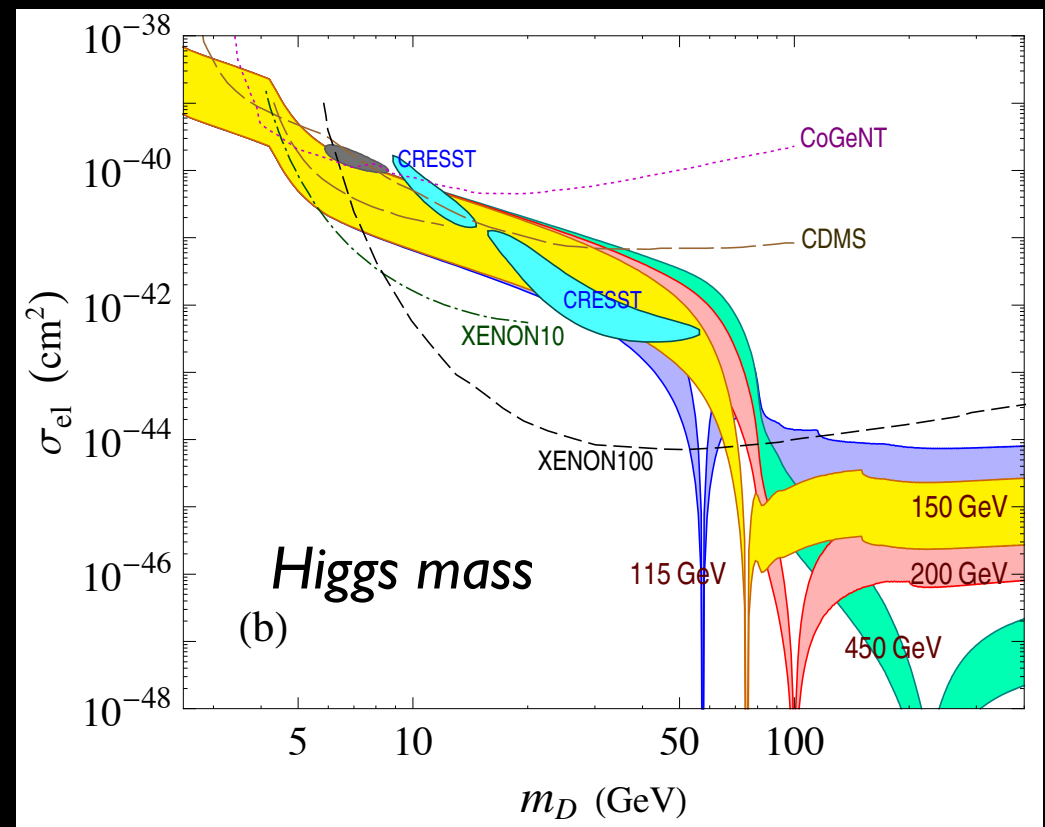
Silveira, Zee 1985

“Higgs portal scalar dark matter”

Andreas, Hambye, Tytgat 2008



Andreas, Arina, Hambye, Ling, Tytgat 2010



He, Tandean 2011

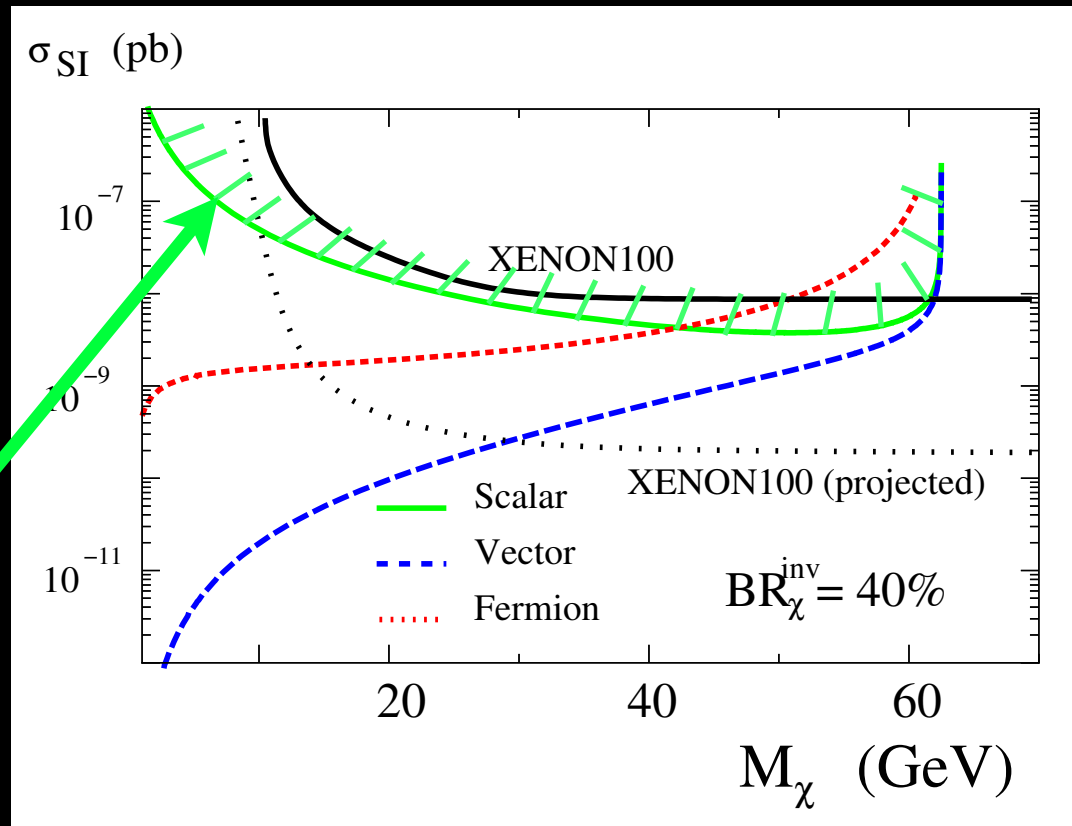
Minimalist dark matter

do not confuse with minimal dark matter

Constraints from the LHC: a 125 GeV Higgs is not 99.2% invisible

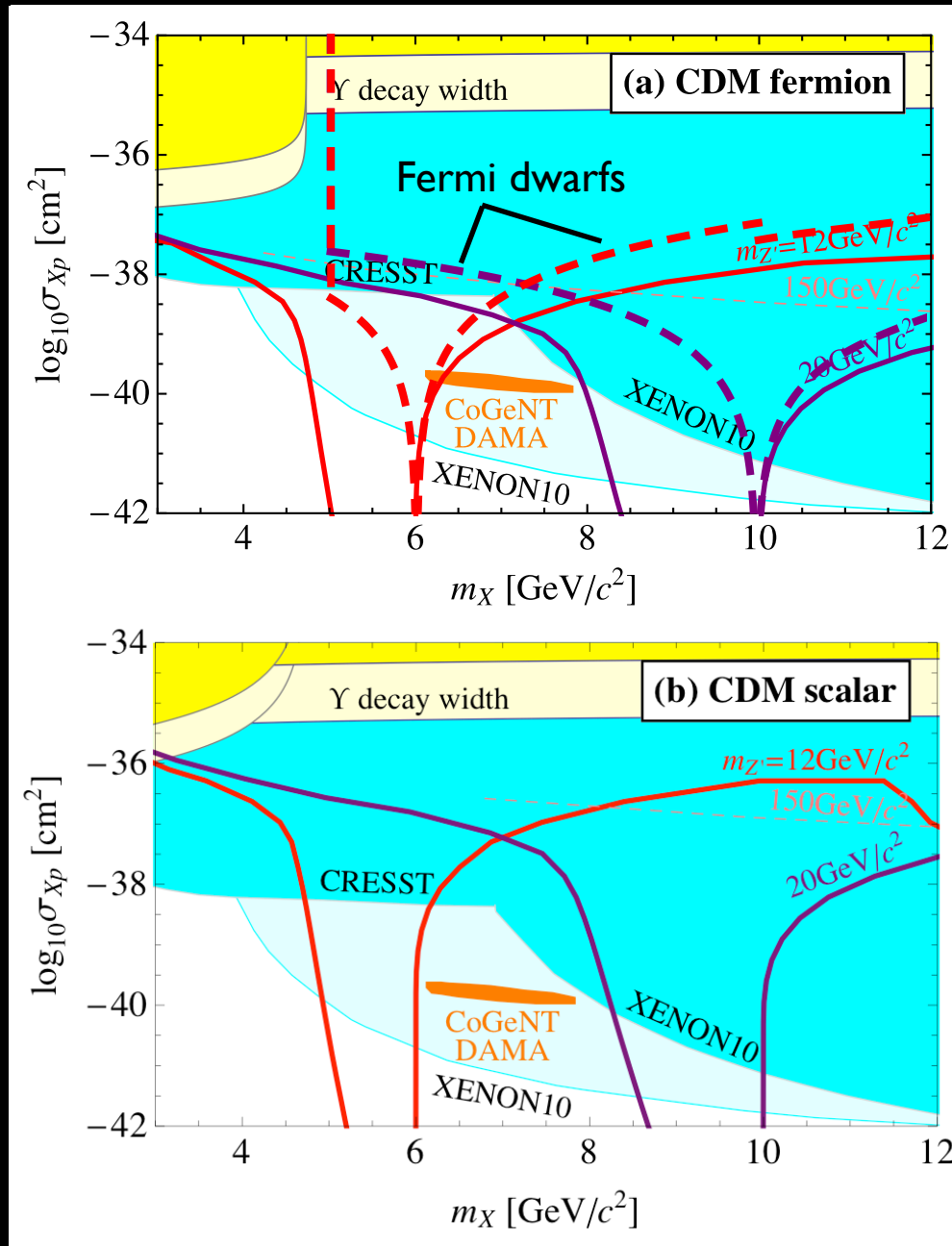
Light
WIMP
region

LHC limit



Djouadi, Falkowski, Mambrini, Quevillon 2012

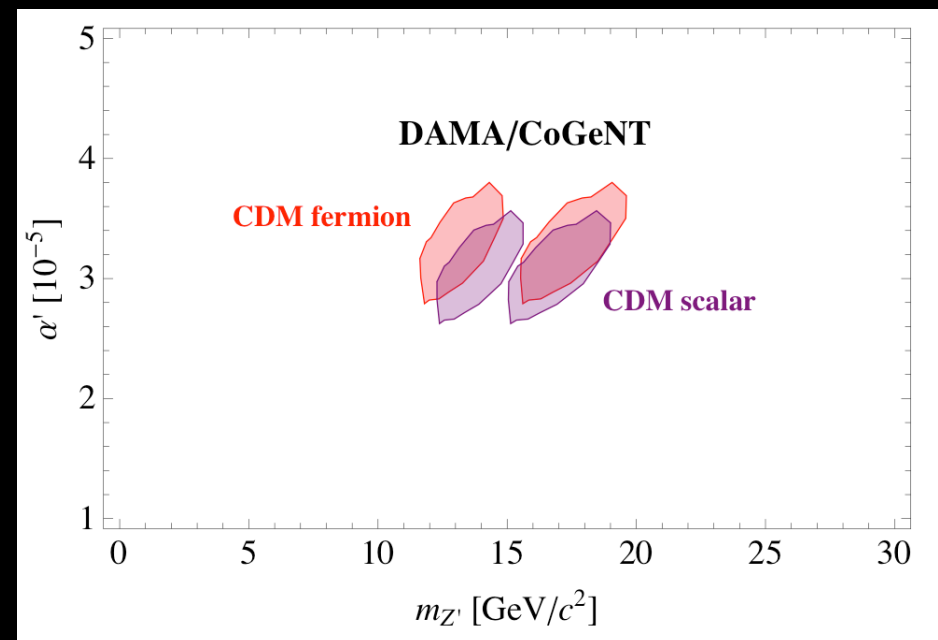
Light WIMPs with light Z' boson



Example: Leptophobic Z'

- An extra U(1) gauge boson Z' coupled to quarks but no leptons, with no significant kinetic mixing
- Works for $m_{Z'} \sim 10\text{-}20 \text{ GeV}$ and $\alpha' \sim 10^{-5}$

Gondolo, Ko, Omura 2011



Astrophysics model

$$\left(\begin{array}{c} \text{recoil} \\ \text{rate} \end{array} \right) = \left(\begin{array}{c} \text{particle} \\ \text{physics} \end{array} \right) \times \boxed{\text{(astrophysics)}}$$

How much dark matter comes to Earth?

$$\text{(astrophysics)} = \overbrace{\rho}^{\text{Local halo density}} \int_{v > v_{\min}(E)} \overbrace{\frac{f(\vec{v}, t)}{v}}^{\text{Velocity distribution}} d^3v$$

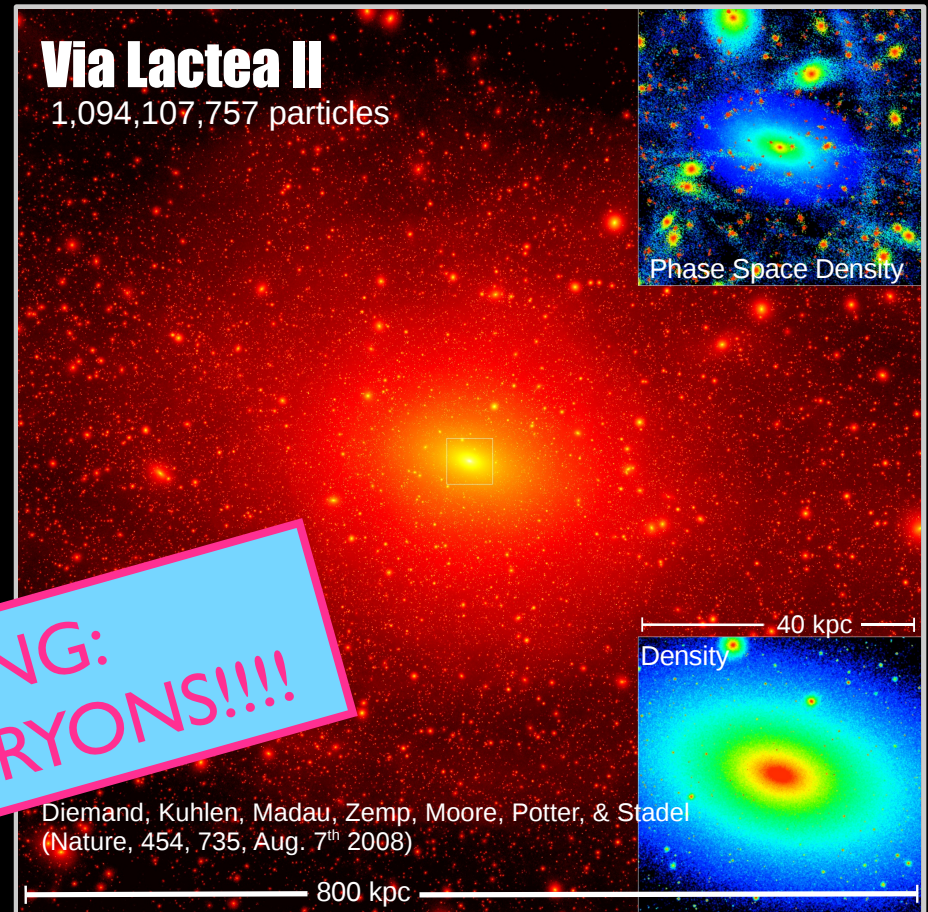
Minimum speed to impart energy E , $v_{\min}(E) = (ME/\mu + \delta)/\sqrt{2ME}$

Astrophysics model: velocity distribution

We know very little
about the dark matter
velocity distribution



**WARNING:
NO BARYONS!!!!**



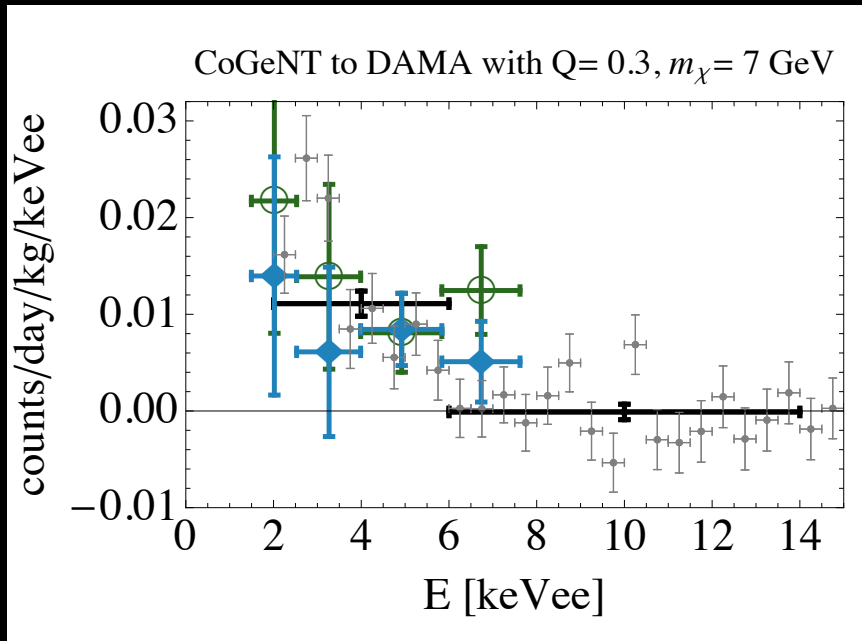
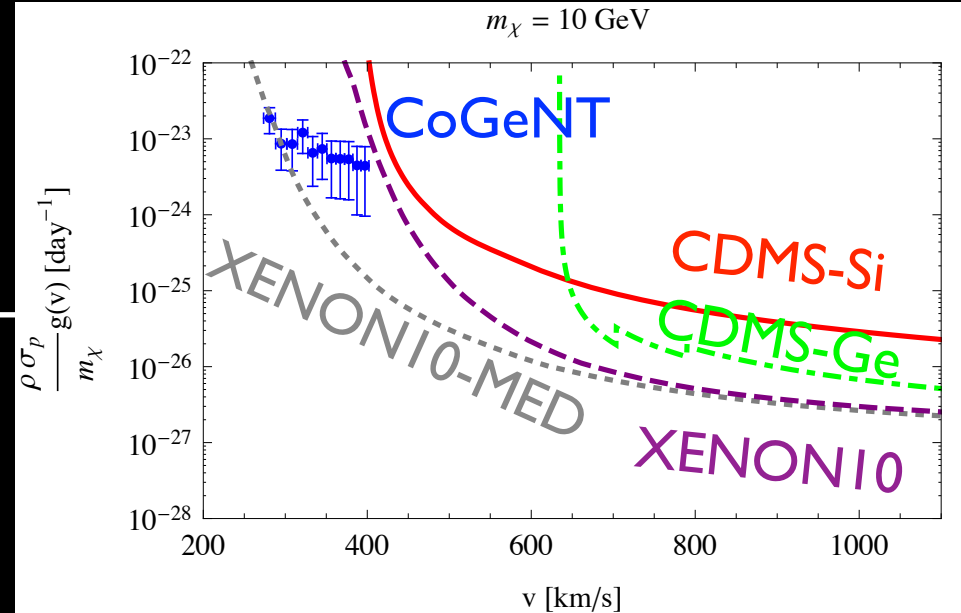
*Cosmological N-Body
simulations including
baryons are challenging*

Astrophysics-independent approach

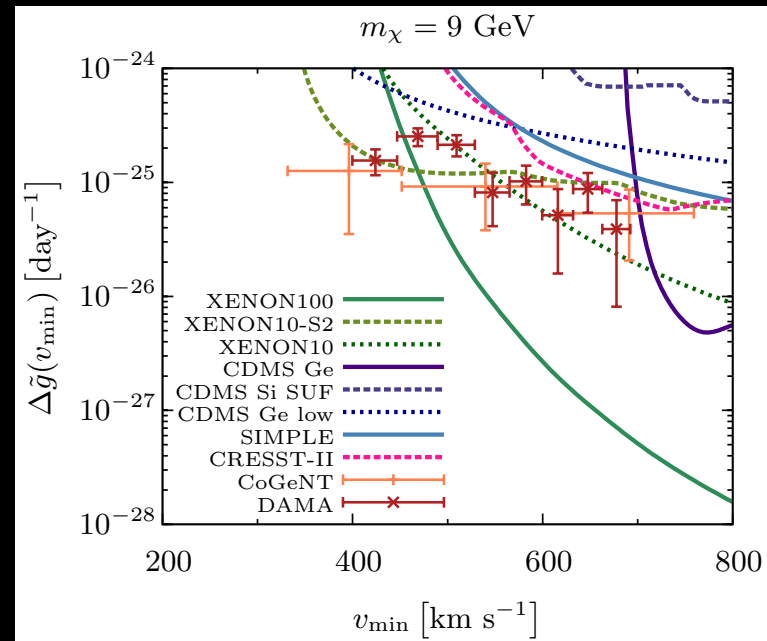
Fox, Liu, Weiner 2011

Astrophysics factor

$$\frac{\rho_\chi \sigma_{\chi p} c^2}{m_\chi} \int_v^\infty \frac{f(v')}{v'} dv'$$



Fox, Kopp, Lisanti, Weiner 2011



Frandsen et al 2011

Astrophysics-independent approach

Include energy dependence of efficiency and energy response function.

Gondolo Gelmini 1202.6359

$$\frac{dR}{dE'} = \int_0^\infty \mathcal{G}(E', E) \frac{dR}{dE} dE$$

Measured energy

*Effective energy
response function*

Recoil energy

Change variables:

$$v_{\min} = \sqrt{\frac{m_T E}{2\mu^2}}$$

*Minimum WIMP speed
to impart recoil energy E*

$$\tilde{\eta}(v_{\min}) = \sigma_{\chi p} \frac{\rho_\chi}{m_\chi} \int_{v_{\min}}^\infty \frac{f(\mathbf{v})}{v} d^3v$$

*Halo-independent factor
accessible to experiments*

Astrophysics-independent approach

Include energy dependence of efficiency and energy response function.

Gondolo Gelmini I 202.6359

Expected rate in energy interval $[E_1, E_2]$

$$R_{[E'_1, E'_2]} = \int_0^\infty \mathcal{R}_{[E'_1, E'_2]}(v_{\min}) \tilde{\eta}(v_{\min}) dv_{\min}$$

Response function

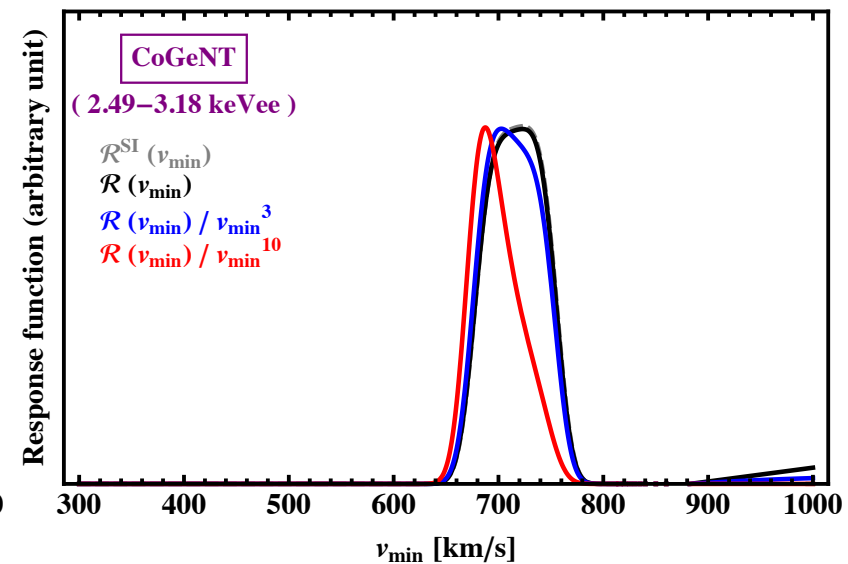
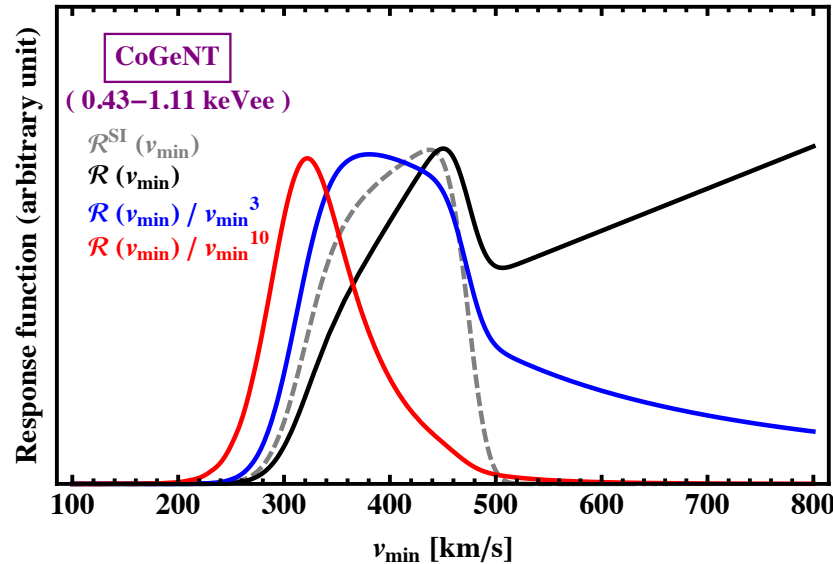
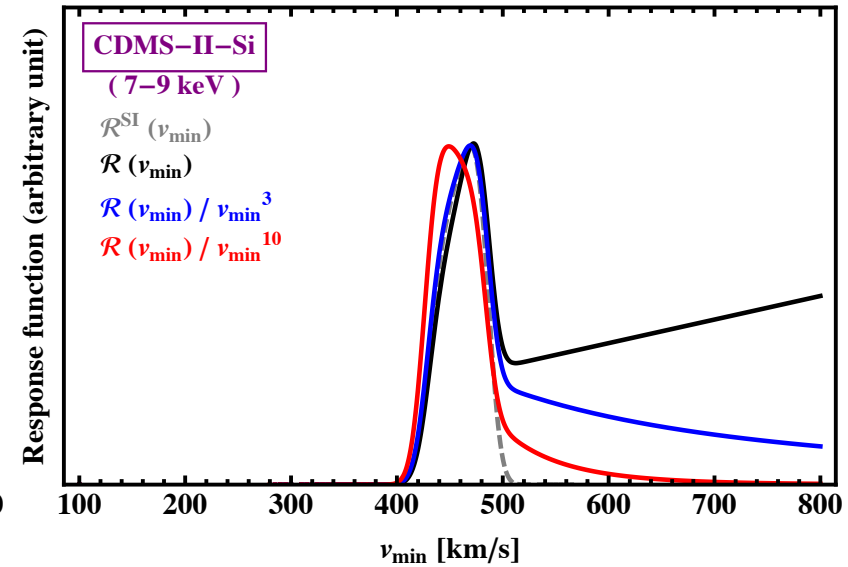
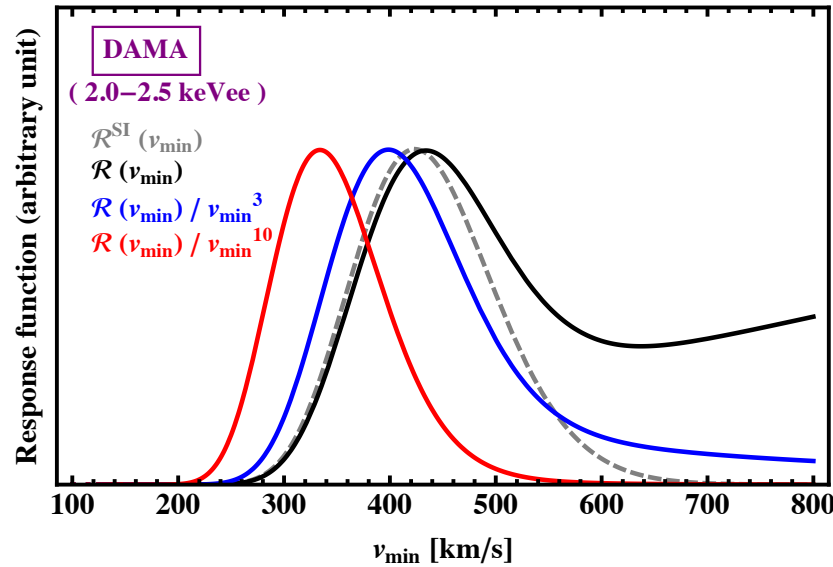
Estimate of halo-independent factor in velocity interval $[v_1, v_2]$

$$\bar{\tilde{\eta}}_{[v_1, v_2]} = \frac{R_{[E'_1, E'_2]}^{\text{measured}}}{\int_0^\infty \mathcal{R}_{[E'_1, E'_2]}(v_{\min}) dv_{\min}}$$

$$\tilde{\eta}(v) < \frac{R_{[E'_1, E'_2]}^{\text{upper limit}}}{\int_0^v \mathcal{R}_{[E'_1, E'_2]}(v_{\min}) dv_{\min}}$$

Astrophysics-independent approach

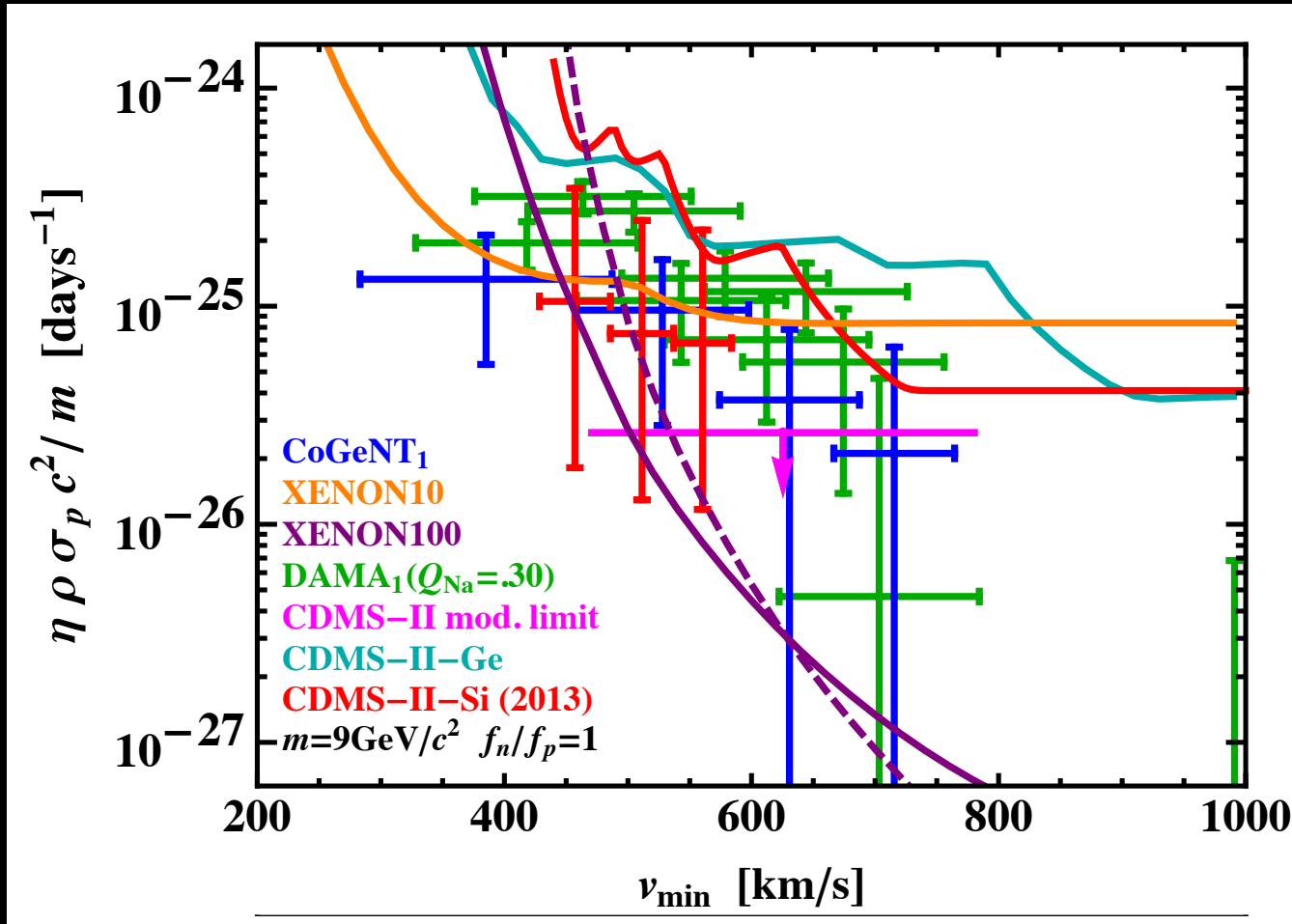
Include energy dependence of efficiency and energy response function.



Del Nobile, Gelmini, Gondolo, Huh 2013

Astrophysics-independent approach

Spin-independent interactions $\sigma_{\chi A} = A^2 \sigma_{\chi p} \mu_{\chi A}^2 / \mu_{\chi p}^2$



Halo modifications alone cannot save the SI signal regions from the Xe bounds

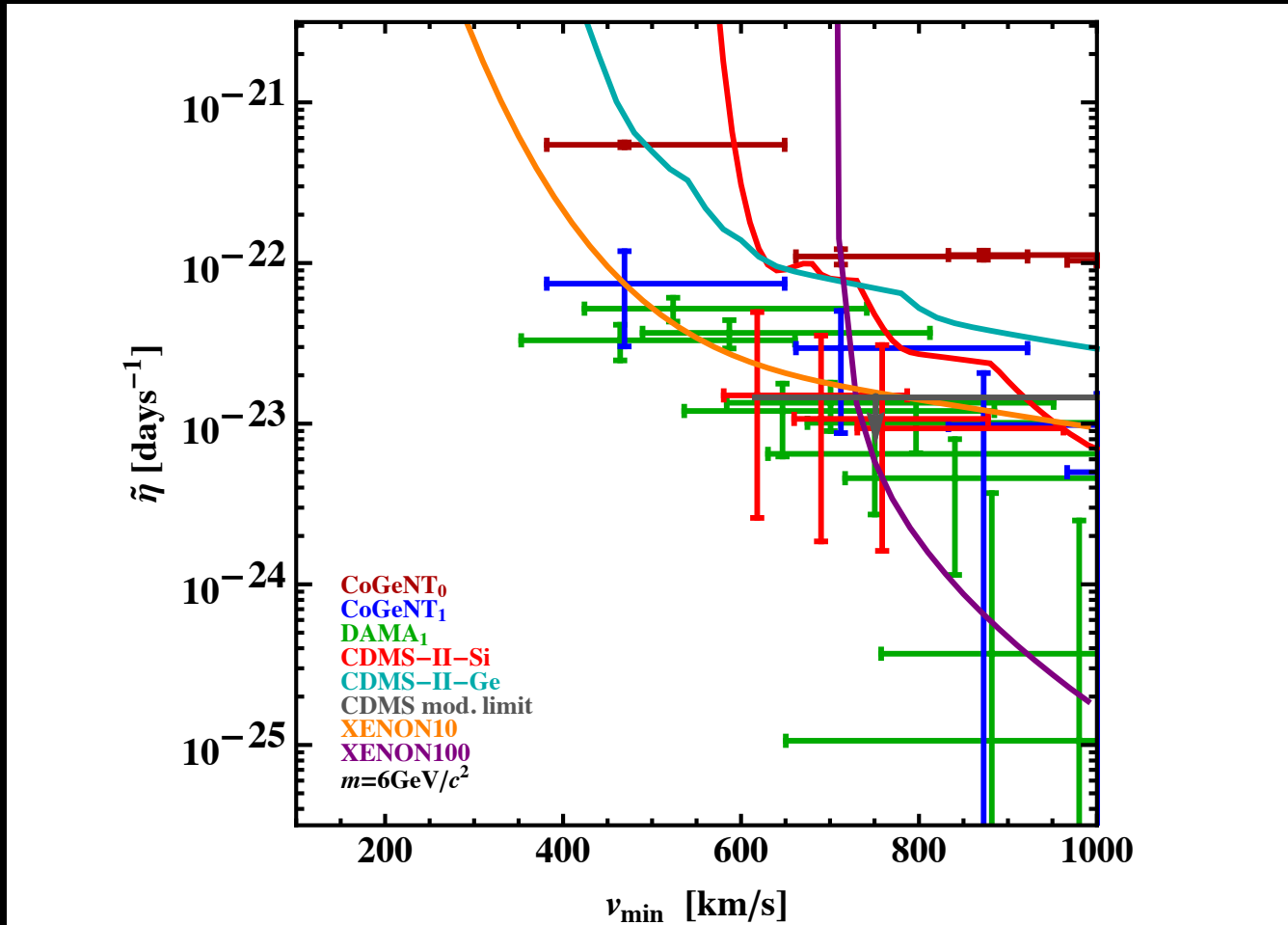
CDMS-Si event rate is similar to annual modulated rates

Del Nobile, Gelmin, Gondolo, Huh 2013

Still depends on particle model

Astrophysics-independent approach

Anomalous magnetic moment dark matter



Halo modifications alone cannot save the MDM signal regions from the Xe bounds

CDMS-Si event rate is similar to annual modulated rates

Del Nobile, Gelmin, Gondolo, Huh 2013

Still depends on particle model

Summary

- The thermal WIMP hypothesis is under strong scrutiny, especially at masses ~ 10 GeV (light dark matter).
- Controversial evidence for direct detection of light dark matter particles (maybe be backgrounds).
 - Halo-independent analyses show that recent CDMS-Si events occur at a rate smaller than the CoGeNT/DAMA modulation amplitudes.
- LHC and indirect searches (γ , CMB, e^+) place strong constraints on models of ~ 10 GeV thermal WIMPs.
 - Light supersymmetric particles may still be possible beyond the MSSM. Non-supersymmetric models include a 10-20 GeV Z' boson coupled to quarks but not leptons.